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A LAPLACE TRANSFORM AMPLITUDE FUNCTION GENERATOR UTILIZING A THIN FILM SEMI-CONDUCTOR

James E. Brown, Jr.

Army Missile Command Redstone Arsenal, Alabama

31 July 1972

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by

James E. Brown, Jr.

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U.S. ARMY MISSILE COMMAND

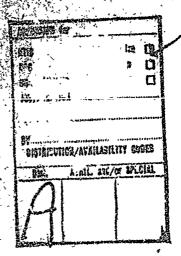
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James E. Brown, Jr.

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Systems Engineering and Integration Office
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and Missile Systems Laboratory
US Army Missile Command
Redstone Arsenal, Alabama 35809

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ABSTRACT

The characteristics of many systems can be predetermined by application of an analog. This report was developed to produce a better tool in the area of the electric field analog. It develops as a straightforward proof of the analog existence with the main body being experimental. The experimental area develops in normal form with early familiarization methods through various phases to the final result. The semiconductor can be used with more consistency, and better results, than any present guaranteed device on the market.

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LIST OF SYMBOLS

đ	Radial	distance	from	center	contact	to	measured	point	on	а
	wafer									

- E Voltage applied to wafer center contact
- $\mathbf{E}_{\mathbf{a}}$ Actual voltage at a measured point
- $\mathbf{E}_{\mathbf{m}}$ Measured voltage

- G Network transfer function
- Kn Wafer contact separation per frequency unit
- ${\bf K_1}$ Constant to calculate a logarithm curve from experimental data
- K₂ Scale factor relating Laplace function to experimental data
- K₃ Scale factor relating the experimental voltage reference to the Laplace function
- m Distance between wafer contacts
- p Pole in the X function and s plane
- r Zero in the X function and s plane
- U Real component of W
- V Imaginary component of W
- W Force exerted by \(\lambda\) on a unit charge in the Z plane
- Z Complex function made up of x and y. Also used to define the plane containing x and y
- α Angle related to r
- β Angle related to p
- € Relative dielectric constant
- ϵ_0 Permittivity of free space

- θ Angle of \overline{W} relative to the x axis in Z
- λ Charge at the center of the Z plane
- Equipotential lines
- X Work required to move a charge in the Z plane
- ψ Streamlines

CHAPIER I

INTRODUCTION

The evolution of modern technology over the past three decades has been made possible by the development of computation and simulation capability. The first devices to be used on a large scale were primarily those of an analog type. The drift and source power sensitivities were accepted and compensated for with either manual calculation or adjustment.

As 'he decade of the fifties evolved, the digital computer became of age from the clumsy tube, drum memory, meat cooler container type of the 1950 vintage to the transistor discrete component type of the 1960 period.

The present mechanization in the digital and analog circuit area is the expicenductor integrated circuit unit. The area of simulation has moved to the combining of analog and digital techniques in the "hybrid configuration."

With the advent of this type of operation, the ready transfer from one technique to another on a real time basis becomes necessary. Many of the present thin sheet analog devices are impractical to automate while others require a complete servo system to generate the necessary functions. The purpose of this report is to investigate one possible method to alleviage this situation.

It should be remembered throughout this report that the thin film analogy has been used for a number of applications. The requirements

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for homogeneous, uniform, and isotropic material together with accurate contact take-off are universal and not limited to the discussion of a particular function.

This has been pointed out by Reynolds in his thesis [1] and amplified in a number of discussions and papers by Huebschmann [2]. While Reynolds dealt with the analog in great detail and indicated the application to function generation, the primary purpose of this report is to investigate a method rather than prove application in all facets as an analog.

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According to Karplus [3], the first conductive sheet was demonstrated by Kirchoff in 1845 and utilized copper. A number of metallized type devices have been developed for various products. In 1875 an electrolyte was utilized for development of various models which was dominant until the development of Teledeltos paper in 1948. There were some successful developments before Teledeltos; one of the most notable was Kayan's [4] use of metallic conductive sheets.

The use of low-resistivity metallic sheets presents one limit of the application which requires reading of potentials to a high degree of accuracy. This probably accounts for the low level of application until the development of Teledeltos paper.

The Teledeltos paper has been widely used despite the fact that it has poor characteristics for the application. It is susceptible to puncture with the probe pressure and to tear with application of

 $[\]frac{1}{N}$ Numbers in brackets refer to similarly numbered references in the bibliography.

stress. It can however be purchased reasonably cheap and the widths of approximately 3 feet help to resolve the problems of an "infinite" sheet. Teledeltos paper was used for investigation in a report by Huebschmann and Pender [2] in 1970 together with other materials. This report essentially verified findings as to shortcomings for the application.

The second secon

Thin conductive sheets have been used as analogues to determine behavior in a number of fields related to physical phenomena. The materials used as discussed have varied in type and apparatus mechanization in a number of ways. Previous investigations by ICING Research Staff [5] in 1953 indicate that resistivity ranges from 100 to 100,000 ohms per square are suitable for this application. The errors in utilization of this technique can be separated; this report deals with a number of these.

The uniformity throughout a particular sheet of material and the location accuracy of source, sink, and measurement points are of primary concern. This report deals with the possibility of utilizing a semiconductor wafer with its uniform conductivity and with microcircuit location accuracy for application to the problem.

The primary advantage of using the semiconductor thin film together with possible deposition of contacts, if accuracy requirements can be met, is in the area of minimum cost units which possibly could be stacked and switched to generate any desirable function. Electronic switching could provide a hybrid interface for use with digital machines where application of the analog becomes the most efficient method of investigation.

A brief discussion of the electric field with the final form of its potential function will be developed simultaneously with a corresponding Laplace equation to prove the validity of the analogy.

A discussion of various units now in existence together with their size, cost, and accuracy data will be furnished and a comparison will be made as to what might be expected from use of semiconductor sheets.

A chapter will be devoted to experiments which have been made to investigate the application and limitations and phenomena which were observed. A final discussion will be furnished on conclusions which can be drawn from this work and a method will be suggested for further pursuit or discard of the approach.

CHAPTER II

DEVELOPMENT OF THE POTENTIAL ANALOG

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In discussing the potential analogy dealt with in this report, a cursory review of the complex potential area is adequate. To review the complex potential and indicate validity of the mathematical approach, a limited review in a narrow area of complex variables is a necessity. Consideration of the complex variable theory will be inserted at various points throughout the discussion for the purpose of continuity. The section will be developed by establishing the equation for an infinite sheet and showing it to be identical to the investigated devices.

Chen [6] presents a more detailed discussion than that presented in this study and is the primary reference for this work.

If we place an infinitely long line through the origin of the Z plane, Figure 1, and define the charge on it as λ along the length of line, it will produce an electric field in the Z plane.

We define \overline{W} as the force on a unit charge, of the same polarity as the line, due to λ . This by definition becomes the electric field intensity of charge λ .

The magnitude of this force is known to be

$$\left|\widetilde{w}\right| = \frac{\lambda}{2 \pi \epsilon |Z|}$$

where Z is the distance from the line charge in meters, ϵ is the relative dielectric constant,

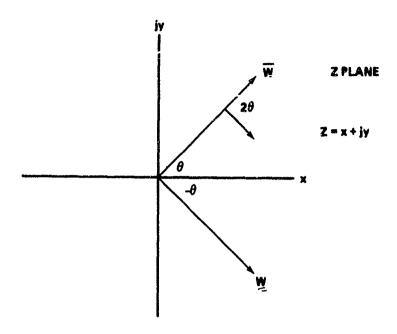


Figure 1. Line charge in the Z plane.

$$\epsilon_0 = \frac{10^7}{4\pi c^2}$$
 , and

 $|\overline{W}|$ is in newtons.

Because the force is along a direction of the vector in Figure 1, we can specify

$$\overline{W} = |\overline{W}| / \theta = \frac{\lambda}{2\pi \epsilon |Z|} / \theta$$

but,

$$\underline{\theta} = 1\underline{\theta} = \frac{|z|}{|z|}\underline{\theta} = \frac{z}{|z|}$$

and

$$\widetilde{W} = \frac{\lambda Z}{2r \in |z|^2} ;$$

however.

$$|z|^2 = z \overline{z}$$

where $\overline{z} = complex conjugate of Z, and$

$$\overline{W} = \frac{\lambda}{2\pi e \overline{z}} \qquad , \tag{1}$$

which represents the actual electric field due to λ . The conjugate

$$W = \frac{\lambda}{2\pi e Z} \qquad . \tag{2}$$

At this point it is necessary to investigate these two functions considered as complex variables.

We consider

$$W = f(Z)$$

$$Z = x + jy$$

$$W = U + jV = f(x + jy)$$

then

$$U = U(x, y)$$

$$V = V(x, y)$$

From this,

$$W = \frac{1}{Z} = \frac{1}{x + jy} \frac{(x - jy)}{(x - jy)}$$

$$=\frac{x}{x^2+y^2}+\frac{y(-y)}{x^2+y^2}$$

$$U = \frac{x}{x^2 + y^2} \tag{3}$$

$$V = \frac{-y}{x^2 + y^2} . (4)$$

This procedure is used to determine relationships to analyticity of the two functions in Z and hence the following definition.

A function is analytic throughout a region R of the Z plane if its derivative dW/dZ exists at every point in the region and the function is single valued throughout R.

Define

$$\frac{dW}{dZ} = \frac{1 \text{im}}{\Delta Z \to 0} \frac{\Delta W}{\Delta Z}$$

There is more than one way to let $\Delta Z \to 0$. If we consider $\Delta y \to 0 \text{ initially, then}$

$$\frac{dW}{dZ} = \frac{1im}{\Delta x \to 0} \quad \frac{\Delta W}{\Delta x + 0} = \frac{\Delta W}{\Delta x}$$

or if $\Delta x \rightarrow 0$ initially,

$$\frac{dW}{dZ} = \frac{1 \text{ im}}{\Delta y \to 0} \quad \frac{W}{0 + 1 \Delta y} = \frac{1}{1} \frac{\Delta W}{\Delta y}$$

If the derivative dW/dZ exists at any point, it must have a unique value at that point independent of the direction of approach. Hence for a derivative to exist

$$\frac{\Delta W}{\Delta x} = \frac{1}{j} \frac{\Delta W}{\Delta y}$$

but

$$\frac{\partial w}{\partial x} = \frac{\partial v}{\partial x} + j \frac{\partial v}{\partial x}$$

and

$$\frac{1}{j}\frac{\partial W}{\partial y} = \frac{\partial V}{\partial y} - j\frac{\partial U}{\partial y}$$

from which

$$\frac{\alpha U}{cx} = \frac{\alpha V}{cy} \tag{5}$$

$$\frac{\alpha U}{\alpha y} = -\frac{\alpha V}{\alpha x} \quad . \tag{6}$$

These Cauchy Reimann equations are normally considered necessary but not sufficient conditions to guarantee the existence of a derivative. In this work, however, Equation (5) or Equation (6) can be considered as sufficient.

We can now investigate:

$$\overline{W} = \frac{1}{\overline{z}} = \frac{1}{x - jy} \frac{(x + jy)}{(x + jy)} = \frac{x}{x^2 + y^2} + j \frac{y}{x^2 + y^2}$$

$$\overline{W} = U + jV$$

$$U = \frac{x}{x^2 + y^2}$$

$$\frac{\alpha U}{\alpha y} = \frac{-2 xy}{\left(x^2 + y^2\right)^2}$$

$$\frac{\alpha U}{\alpha x} = \frac{y^2 - x^2}{\left(x^2 - y^2\right)^2}$$

and

$$V = \frac{y}{x^2 + y^2}$$

$$\frac{\partial V}{\partial y} = \frac{x^2 - y^2}{\left(x^2 + y^2\right)^2}$$

$$\frac{\partial V}{\partial x} = \frac{-2xy}{\left(x^2 + y^2\right)^2}$$

Neither of the Cauchy-Reimann equations hold and therefore $1/\overline{z}$ is not analytic. From Equations (3) and (4) for W=1/Z,

$$U = \frac{x}{x^2 + y^2}$$

$$\frac{\alpha U}{\alpha y} = \frac{-2xy}{\left(x^2 + y^2\right)^2}$$

$$\frac{\alpha U}{\alpha x} = \frac{y^2 - x^2}{\left(x^2 + y^2\right)^2}$$

$$V = \frac{-y}{x^2 + y^2}$$

$$\frac{\partial V}{\partial y} = \frac{y^2 - x^2}{\left(x^2 + y^2\right)^2} \qquad \frac{\partial V}{\partial x} = \frac{2xy}{\left(x^2 + y^2\right)^2}$$

and

$$\frac{\alpha U}{\alpha x} = \frac{\alpha V}{\alpha y}$$
 $\frac{\alpha U}{\alpha y} = \frac{-\alpha V}{\alpha x}$

Then 1/Z is an analytic function which denotes analyticity at all but the functions own singular points which in this case exists at $0 + j \ 0$.

Let it suffice in further development of the function W = 1/Z, where Z = x + jy, to state that the integral of an analytic function also satisfies the Cauchy-Riemann equations and is analytic over the specified region.

Figure 2 illustrates the movement of a unit charge a distance of . dZ over the path Z_0 , Z. From Equation (2) the force at Z is

$$W = \frac{\lambda}{2\pi \epsilon Z}$$

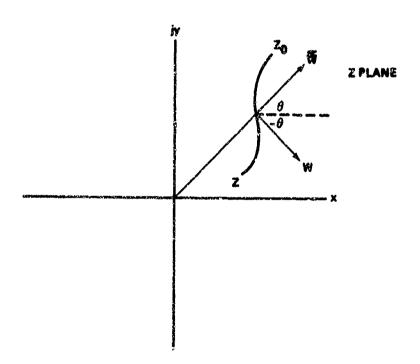


Figure 2. Force components in the Z plane.

Since we are moving counter to the force or field intensity a distance of dZ, the work or complex potential to move over the path \mathbf{Z}_0 to Z is

$$X(Z) = \int_{Z_0}^{Z} - W(Z) dZ = \int_{Q}^{Z} \frac{-\lambda}{2\pi\epsilon Z} dZ$$

$$= \frac{-\lambda}{2\pi\epsilon} \left(\ln Z + \ln Z_0 \right)$$

$$= \frac{-\lambda}{2\pi\epsilon} \ln \frac{Z}{Z_0} .$$

We can choose Z_0 as a reference point of 1 or the point where $X(Z_0) = 0$, then

$$\chi(z) = \frac{-\lambda}{2\pi\epsilon} \ln z$$

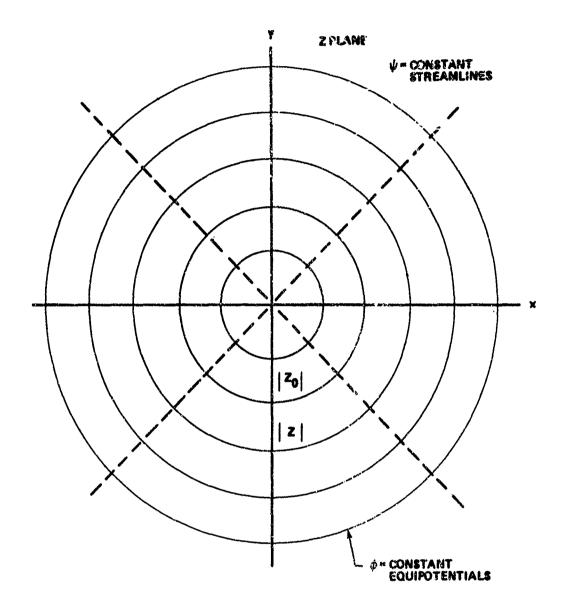
$$= \frac{-\lambda}{2\pi\epsilon} \ln|z| e^{j\theta}$$

$$\chi(z) = \theta(x, y) = \phi(x, y) + j\psi(x, y) \qquad (7)$$

$$\phi = \frac{-\lambda}{2\pi\epsilon} \ln |Z| = \text{equipotential}$$
 (8)

$$\psi = \frac{-\lambda}{2\pi\epsilon} e^{j\theta} = \text{streamline} \qquad . \tag{9}$$

Figure 3 presents a plot in the Z plane of Equations (8) and (9) with various |Z| and θ held constant. It can be seen that Equation (8) represents equal potential lines at radius equal to |Z|. Because Z_0 was chosen equal to 1, measurements from that point for $|Z| < |Z_0|$ can be considered positive potential lines and those with $|Z| > |Z_0|$ as negative potential contours. The manipulation of $Z_0 = 1$ implies $Z_0 = 1$ and hence ψ would be referenced from a given angle, in this case chosen as the positive x. The j $\psi(x, y)$ in Equation (7) as compared to $\phi(x, y)$ indicates the orthogonality of the streamlines and equipotentials.



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Figure 3. Electric field plot with equipotentials and streamlines.

For a single positive line charge at $P = x_p + jy_p$, the substitution Z = Z - p can be made and

$$X(Z^{\dagger}) = \frac{1}{2\pi\epsilon} \ln \frac{1}{Z^{\dagger}} + \frac{\lambda}{2\pi\epsilon} \ln Z_0^{\dagger}$$

$$X(Z) = \frac{\lambda}{2\pi\epsilon} \ln \frac{1}{Z-p} + \frac{\lambda}{2\pi\epsilon} \ln (Z_0 - p)$$

Because

$$- W = -(W_1 + W_2 + ... + W_n)$$

for several line charges of mixed polarity and equal value in the Z plane,

$$X(Z) = \frac{\lambda}{2\pi\epsilon} \ln \frac{\left(Z - r_1\right)\left(Z - r_2\right) \cdot \cdot \cdot \left(Z - r_m\right)}{\left(Z - r_1\right)\left(Z - r_2\right) \cdot \cdot \cdot \left(Z - r_m\right)} + C \qquad (10)$$

with

$$C = -\frac{\lambda}{2\pi\epsilon} \ln \frac{\left(-r_1\right)\left(-r_2\right) \cdot \cdot \cdot \left(-r_m\right)}{\left(-p_1\right)\left(-p_2\right) \cdot \cdot \cdot \left(-p_m\right)}$$
 (10a)

where $Z_0 = 0$.

$$z - r_{1} = |z - r_{1}| e^{\alpha 1}$$

$$z - r_{2} = |z - r_{2}| e^{\alpha 2}$$

$$\vdots$$

$$z - r_{m} = |z - r_{m}| e^{\alpha m}$$

$$z - r_{1} = |z - r_{1}| e^{\beta 1}$$

$$z - r_{1} = |z - r_{1}| e^{\beta 1}$$

$$z - r_{2} = |z - r_{2}| e^{\beta 2}$$

$$\vdots$$

$$\vdots$$

$$z - r_{n} = |z - r_{n}| e^{\beta n}$$

$$x(z) = \frac{\lambda}{2\pi\epsilon} \left(\ln|z - r| + \ln|z - r_{2}| + \dots + \ln|z - r_{m}| \right)$$

$$- \ln|z - r_{1}| - \ln|z - r_{2}| - \dots - \ln|z - r_{n}| \right)$$

$$- \frac{\lambda}{2\pi\epsilon} \left(\ln|r_{1}| + \ln|r_{2}| + \dots + \ln|r_{m}| - \ln|r_{1}| \right)$$

$$+ \frac{\lambda}{2\pi\epsilon} \left(\alpha_{1} + \alpha_{2} + \dots + \alpha_{m} - \beta_{1} - \beta_{2} - \dots - \beta_{n} + r \right)$$
 (11)

where r = summation of all angles in C.

Equations (10), (10a), and (11) are the equations for the electric potential function in an infinite thin plane with mixed polarity charges at various locations in the plane.

It now remains to investigate the development of Laplace transforms and their final form to insure that Equations (10), (10a), and (11) are indeed a sufficient analogue. To evaluate the isofulness of the transform, let us consider the type of systems for which it can be utilized. This is intended as a cursory look at the subject sufficient to justify the approach in this report. There is excellent text as the subject complete with tables of the transforms.

Let us state that the Laplace transform can be used in the solution of linear differential equations and these in turn reflect mosc of the physical networks and systems with which we deal. Let the statement stand that by definition a linear system is one for which superposition is valid and that the response to a sum of inputs is equal to the sum of the response of the inputs applied separately.

If we have a differential equation of the form:

$$A_0(x) \frac{d^2y}{dx^2} + A_1(x) \frac{dy}{dx} + A_2(x) y = f_1(x)$$

and letting $\mathbf{y}_1(\mathbf{x})$ and $\mathbf{y}_2(\mathbf{x})$ represent solutions then

$$A_0(x) = \frac{d^2(y_1 + y_2)}{dx^2} + A_1(x) = f_1(x) + f_2(x)$$

$$= f_1(x) + f_2(x) .$$

The classical solution of this type equation is well known; however, the Laplace transform offers a number of advantages such as algebraic solutions together with established tables which make the solution simpler.

The Laplace transform for ε function of f(t) is defined by

$$L[f(t)] = \int_{0}^{\infty} f(t) e^{-st} dt = F(s)$$

As an example, to transform sin Bt:

L sin Bt =
$$\int_{0}^{\infty} \frac{e^{iBt} - e^{-iBt}}{2i} e^{-st} dt$$

$$= \frac{1}{2i} \int_{0}^{\infty} e^{iBt} e^{-st} dt - \int_{0}^{\infty} e^{-iBt} e^{-st} dt$$

$$= \frac{1}{2i} \left[\frac{e^{(iB - s)t}}{iB - s} \Big|_{0}^{\infty} - \frac{e^{-(iB + s)t}}{iB + s} \Big|_{0}^{\infty} \right]$$

$$= \frac{1}{2i} \left[-\frac{1}{iB - s} - \frac{i}{iB + s} \right]$$

$$= \frac{B}{B^{2} + s^{2}} .$$

To deal with electric networks, we could look at transforms of operations:

$$L\left[\frac{\mathrm{df}}{\mathrm{dt}}\right] = \int_{0}^{\infty} \frac{\mathrm{df}}{\mathrm{dt}} e^{-st} dt$$

by letting

and

$$dv = \frac{df}{dt} dt$$

then

$$\int_{0}^{\infty} \frac{df}{dt} e^{-st} dt = f(t) e^{-st} \Big|_{0}^{\infty} + S \int_{0}^{\infty} f(t) e^{-st} dt$$

and

$$L\left|\frac{df}{dc}\right| = -f(0) + S f(s)$$

where

$$\lim_{t\to\infty} f(t) e^{-st} = 0$$

$$L \begin{bmatrix} f \\ f(x) \end{bmatrix} dx = \int_0^\infty e^{-st} dt \int_0^t f(x) dx$$

by letting

$$u = \int_0^t f(x) dx ,$$

$$du = f(t) dt$$

$$v = -\frac{1}{S} e^{-st}$$

and

$$dv = e^{-st} dt$$

then

$$\int_{0}^{\infty} e^{-st} dt \int_{0}^{t} f(x) dx = -\frac{1}{s} e^{-st} \int_{0}^{t} f(x) dx$$

$$+\frac{1}{s}\int_0^\infty e^{-st} f(t) dt$$

and

$$L \begin{bmatrix} f \\ 0 \end{bmatrix} f(x) dx = 0 + \frac{1}{S} \int_{0}^{\infty} e^{-st} f(t) dt = \frac{F(s)}{S} .$$

These transforms are sufficient to allow investigation of electrical elements and consequent development of a network transfer function.

Let us first consider a resistor:

$$v = Ri$$

$$i = \frac{v}{R}$$

$$V(S) = RI(S)$$

$$I(S) = GV(S)$$
.

For a capacitor:

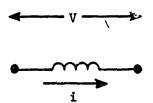
$$V = \frac{1}{C} \int_0^t i dt + V (0)$$

$$i = C \frac{dv}{dt}$$

$$V(S) = \frac{1}{CS} I(S) + \frac{V(0)}{S}$$

$$I(S) = CSV(S) - Cv(0)$$

and finally for an inductor:



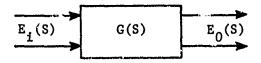
$$V = L \frac{di}{dt}$$

$$i = \frac{1}{L} \int_0^t V dt + i(0)$$

$$V(S) = LS I(S) - Li(0)$$

$$I(S) = \frac{1}{LS} V(S) - \frac{i(0)}{S}$$
..

If we therefore treat the relationship of an input to an output as a transfer function G(S)



then

$$\frac{E_0(S)}{E_1(S)} = G(f)$$

S(S) is written in the form

$$G(S) = \frac{a(s - r_1)(S - r_2) \cdot \cdot \cdot (S - r_n)}{b(s - p_1)(S - p_2) \cdot \cdot \cdot \cdot (S - p_m)}$$

then

$$\ln |G(S)| = \ln \frac{a}{b} + \ln \frac{(S-r_1)(S-r_2) \cdot \cdot \cdot (S-r_m)}{(S-p_1)(S-p_2) \cdot \cdot \cdot \cdot (S-p_n)}$$

which is exactly analogous to Equation (10) where $\ln\frac{a}{b}$ is equivalent to C.

CHAPTER III

PHYSICAL CONSIDERATIONS

There are a number of physical limitations relative to use of the thin sheet analog principle as a practical tool. Since the purpose of this report is related primarily to investigation of a single method, it would do well to discuss others and relate them to various limitations. The limits to be discussed are as follows:

- 1. Size.
- 2. Material.
- 3. Contact Problems.
- 4. Mechanical Measurement Limitations.
- 5. Accuracy.

Operating Complexity.

To discuss these limitations, it is necessary to relate requirements only to an idealized surface with the simple equation of

$$E_{m} = E \ln d \tag{12}$$

where polarity is ignored and

 $E_m = measured voltage$

E = applied potential at the center of an infinite shee.

(resulting in constant current)

d = radial distance from the center point.

All of the equations developed in Chapter II were related to an infinite sheet. This is not practical and destroys the basic investigation which relates to a simple, low priced unit for general use.

If d in Equation (12) is allowed to equal Km, where m = increment of distance measurement and K = number of increments internal, and if the potential is applied at a perfect circular contact on a limited sheet at the maximum k, all internal points are a perfect representation of Equation (12). This is shown in Figure 4.

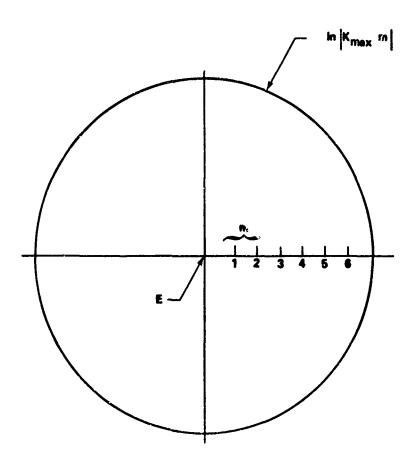


Figure 4. Equipotentials at discrete intervals.

Therefore excluding all other considerations, a circular sheet of any size with applied potentials as defined represent a perfect device in reflecting Equation (12). Other considerations limit the size to some minimum and these considerations will be discussed.

The ICING Research Staff [5] investigated a number of possible conductive materials and their findings can be summarized as follows to eliminate a number of approaches:

- 1. Metal foils are too low in resistivity.
- Metallic coated conductors have unacceptable variations in space conductivity.
- Electrolytic conductors are best applied in tanks and therefore not suitable to the problem.
- 4. Teledeltos paper has disadvantages (previously discussed).
- Conductive paint has some promise but production problems are rather strenuous.

One of the most potent designs available at present is the ESIAC computer [7]. This device uses the Factor Analog method with a large carbon conductor sheet. It requires setting and manipulation of pole-zero probes and with the readout is approximately the size of a large desk. While it is an extremely useful device, it remains larger and more complex than the one being investigated.

One of the problems which becomes obvious is distortion of the field resulting from contacts with conductivity different from the film. The contacts themselves must be negligible relative to the overall area of the sheet. Measuring instrumentation input impedance must be kept large to prevent distortion. Coincident with these problems, the contact and measuring system must avoid the errors of nonpredictable large contact drop.

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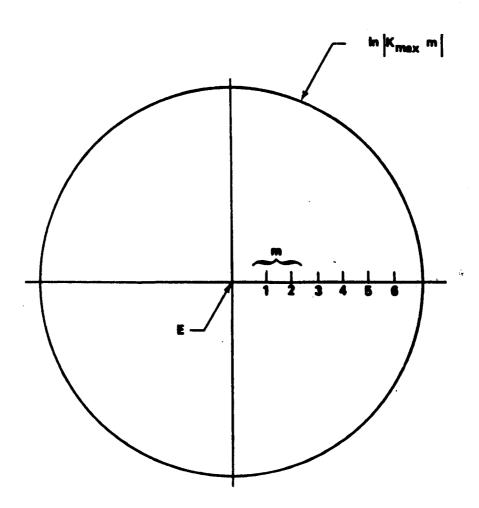


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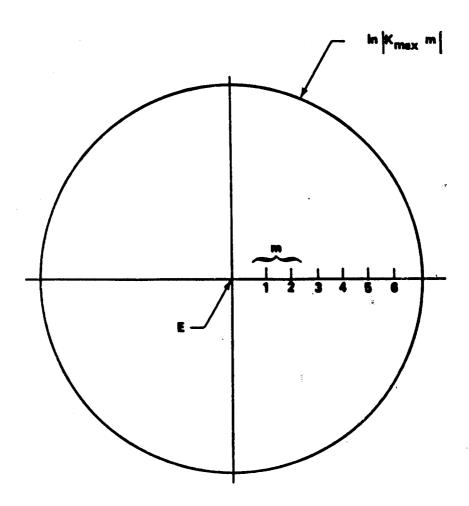


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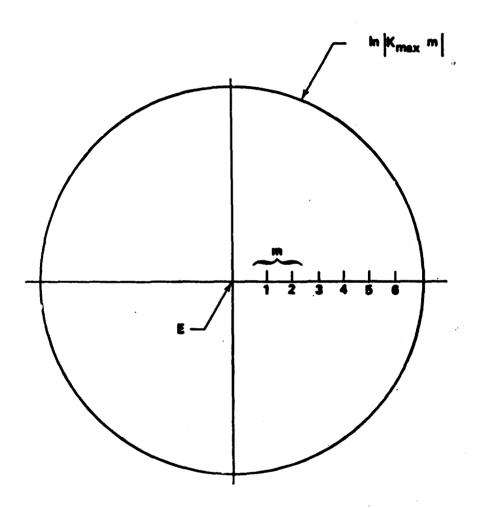


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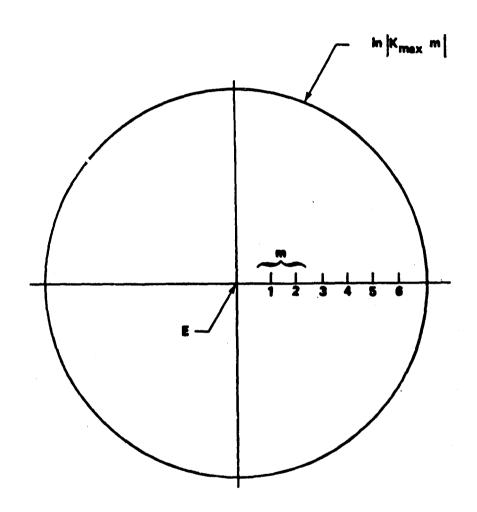


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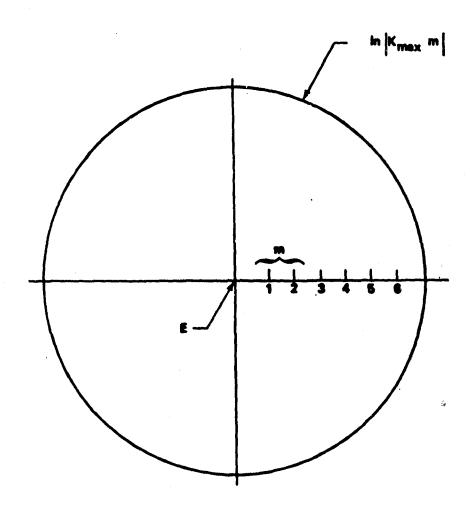


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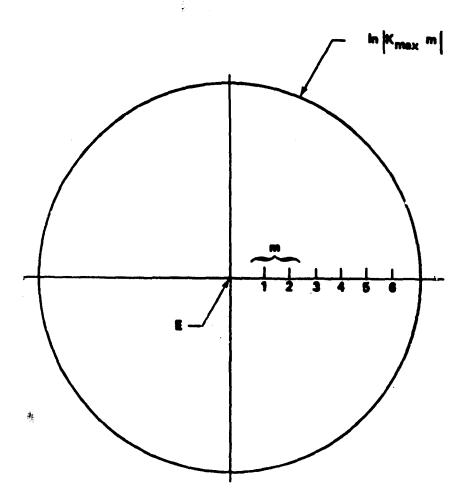


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contact. Where this fixed contact scheme is utilized, the number between the center source and outer ring is of importance because this controls the range of frequencies over which a function can be investigated on a single wafer.

The mechanical accuracy to which a measuring point can be deposited controls the accuracy which can be obtained.

This placement accuracy is of most importance when measurements are made near wafer center. This becomes obvious from Equation (12) if we let $\triangle d$ equal the magnitude of uncertainty. A diagram of the wafer is shown in Figure 4 with necessary constants indicated. Then

$$|E_{m}| = E \ln |d + \Delta d|$$

$$= E \ln |d + 0.001 inch|$$

with a 0.03-inch displacement

$$(Error) = E \ln |0.031| - E \ln |0.030|$$

= E(0.0288) .

If measurement accuracy from an instrumentation aspect is considered, then the total (i.e., predictable drop such as instrument accuracy, distortion resulting from instrument drain, etc.) of all effects must be considered. These effects predominate at the extreme wafer edge where voltage differences are small relative to placement.

Instrument errors will in general follow as a fixed value (i.e., percent full scale) and hence will have significance when considering small voltages.

Then where electrical measurement accuracy only is considered

$$E_{m} = E_{a} + \Delta e$$

where we consider only one direction of error and

 E_{m} = measured voltage

 $E_a = actual voltage$

 $\Delta e = error in voltage.$

If we consider that some percentage of accuracy is required, then at all times

Percent error = $2.88 + \left| \frac{\Delta e}{E_a} \right|$ 100

 $\Delta e = 0.01$ volt is reasonable

Percent error = $2.88 + \frac{1}{E_a}$

Then for a four percent system

$$E_{\min} = 0.893$$

This indicates a worst case feasibility and therefore the final device should approximate three percent near center and nearer one percent at extremes of the wafer.

Most of the present general-use systems satisfy a requirement of ten percent accuracy. Because the device being considered is for even more general use than present units, it would appear that more than sufficient margin exists for attainable material characteristics.

CHAPTER IV

EXPERIMENTAL PROCEDURE AND RESULTS

I. RESISTANCE EXPERIMENTS

A number of familiarization experiments were conducted during the latter part of 1969 through the first part of 1970 using Teledeltos paper with a conductor painted circumference. Measurements of this type were used as a basis for a report by Huebschmann and Pender [2].

A number of silicon wafers were obtained and pick-off measurements were attempted. There was no success in this venture and the generation of the desired logarithmic function could not be obtained. While tungsten tip probes were used and data were obtained, it was too erratic for analysis. It was assumed that poor contacts or the diode effect was the prime causes for poor data, but experimental facilities were not available to verify these assumptions.

It was postulated that some basic measurements should be made on the material in an attempt to determine whether either or both effects existed and which was predominant.

Initial tests were made to determine the effects of instrument insertion and thereby allowed removal of these from consideration. The mechanical arrangement is shown in Figure 5. The voltmeter used, was a Fairchild model 259 and the Ammeter was a Data Technology model DT 360.

Data from this experiment are presented in Table 1 and include results of several repetitive tests made over the total range.

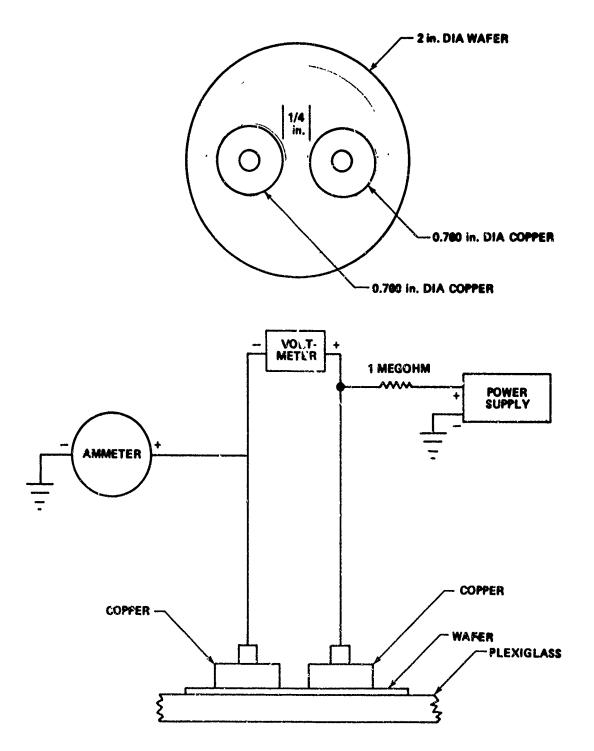


Figure 5. Longitude dimension resistance experiment.

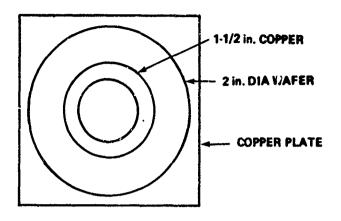
Table 1. Longitude dimension resistance, test 1

Volts	Current (Ma)	Resistance (Kohms)
5.32	0.03	177
8.35	0.05	167
15.4	0.10	154
29.2	0.20	146
69.3	0.50	138
130.9	1.00	130
206.0	1.99	103
285.0	3.14	91
399.0	3.50	114

This experiment indicated that at least some diode effect appeared and that resistance characteristics of the material were too high. It was reasoned that a further test with the mechanical arrangement as shown in Figure 6 would enhance any diode effect.

The data from this experiment are given in Table 2 with presentation in Figures 7 and 8. These data were verified by a number of tests over the total data span. The tunnel effect was observed at precisely 16.7 milliamperes on each test. At this point the voltage across the wafer began to drop and the current increased to the limits of the power supply. Because of facility limits, this phenomenon was pursued no further.

The curve from these data clearly indicated the diode effect and gave direction to part II of the experimental process. It also became evident that lower resistive materials and better contacts were necessary.



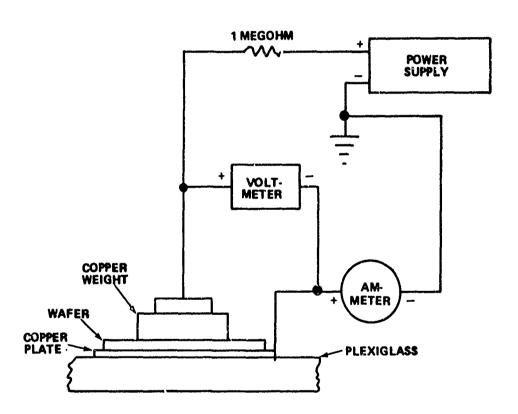


Figure 6. Thin dimension resistance experiment.

Table 2. Thin dimension resistance, test 2

Volts	Current (Ma)	Resistance (Kohms)
5.6	0.03	186
7.5	0.05	150
11.5	0.10	115
17.1	0.20	85
29.7	0.50	59
43.3	1.00	43
66.1	2.02	33
82.8	3.00	28
97.6	4.04	24
109.0	5.18	21
124.7	7.02	18
143.8	10.10	14
155.1	14.00	11
160.6	16.70	10

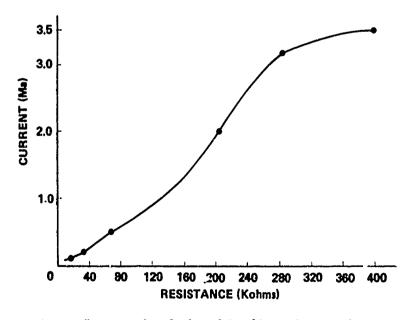


Figure 7. Graph of the thin dimension resistance.

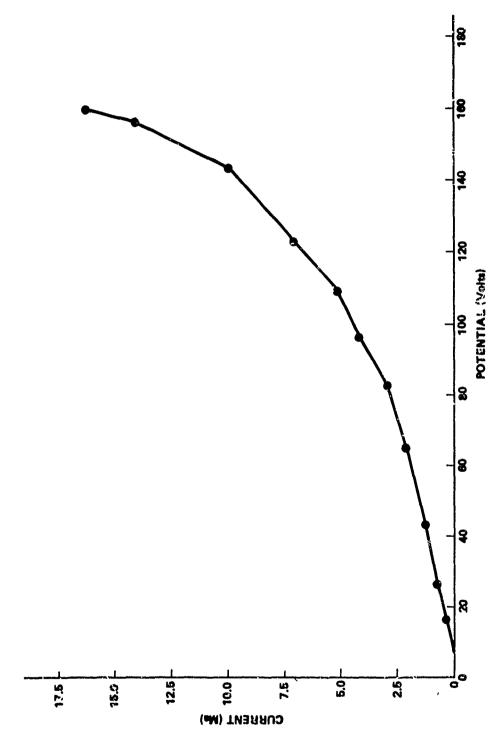


Figure 8. Diode effect in thin dimension experiment.

II. LINEARITY EXPERIMENTS

At this point in experimentation, two wafers were constructed by Astrionics Laboratory of Marshall Space Flight Center. Wafer processing information has been furnished (with proprietary limitations) by this laboratory.

Processing Information:

1. Wafer specifications:

Resistivity 3-5 ohms/centimeter; N type, phosphorous doped

Orientation: 111

Wafer thickness: 7-10 mils

2. Standard clean:

 $85^{\circ}C H_2SO_{4}$: HNO_3 (2:1) 10 minutes

Deionized and distilled (DI) $\mathrm{H}_2\mathrm{O}$ rinse for 10 minutes

Ultrasonic trichloroethylene (TCE) rinse - 10 minutes

Ultrasonic acetone (ACE) rinse - 10 minutes

DI H₂O rinse for 10 minutes

Blow dry with No

3. Pifussion: 980°C furnace

Dopant - Boron

Source - Diborane

Time - 60 minutes

Ohms/centimeter after predip = 27

4. Oxidation: 1150°C

Steam with 0_2 carrier for 40 minutes

- 5. Strip oxide with buffer HC1 etch Ohms/square = 180-200
- 6. Premetal clean

DI H₂O rinse - 10 minutes

ACE ultrasonic rinse - 10 minutes

DI H₂O rinse - 10 minutes

Blow dry with No

- 8. Coat wafers with Kodak thin film photoresist

beam gun. Aluminum thickness = 8KÅ

- 9. Align metallization mask and expose
- 10. Etch away unwanted aluminum
- 11. Ailoy aluminum
 555°C furnace for 5 minutes in N₂ ambient
- 12. Ready to test.

Measurements were made at the Astrionics Laboratory. Photographs of laboratory equipment are shown in Figures 9 through 12. Because of the physical (size) limitations on the probe station, it was necessary to rotate the test sample for various axial readings. In the process of doing this, the first sample was shattered.

In the process of taking rensurements on the second sample, probe movement etched off the center rafer contact before final data on the fourth axis could be completed. An expanded photograph of this wafer is shown in Figure 13. The connections for measurement in circuit diagram form are shown in Figure 14.

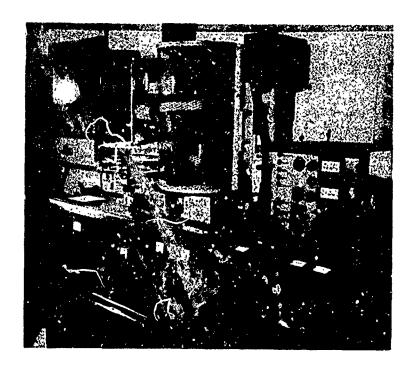


Figure 9. Vacuum chamber.



Figure 10. Testing circuits.

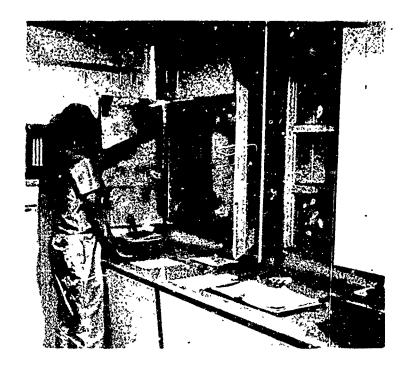


Figure 11. Placing wafers in furnace.

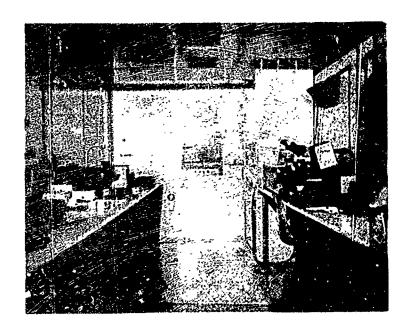


Figure 12. Photolithography room.

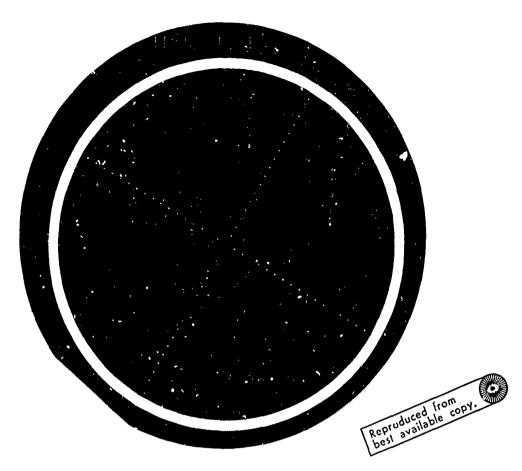


Figure 13. Wafer 2 used in linearity experiments.

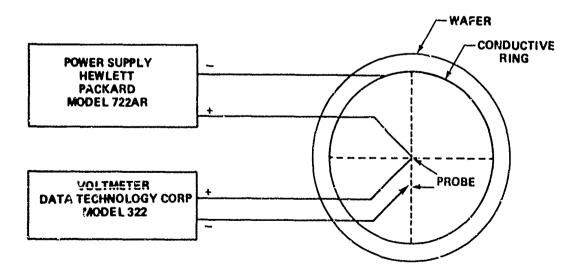


Figure 14. Measurement procedure utilized in linearity experiments.

The initial experimental data are shown in Table 3. Because of limits on the probe station (three probes), the outside conductor drop became a factor. A correction factor was required and applied $(E_c = E_{in} - E_{ring})$ with the final tabular results being listed in Table 4. A column has also been used to generate the average in this table and a plot around this average is shown in Figure 15. The last column in Table 4 indicates the worst percentage variation by point relative to the average. These numbers indicate that the tolerance is well within the desired range from a material standpoint.

The curve plotted in Figure 15 is a distorted representation of the infinite plane because the outer ring was held at an arbitrary potential. This can be corrected for by calculation if there is no distortion other than the ring potential problem at the outer edge. The correction involves one of assuming that the first measurement point from center is correct, calculating an outer ring potential, and correcting each internal point from this.

If points 1 and 2 are satisfactory then:

$$K_1$$
 ln m = 4.797
 K_1 ln 2m = 5.933
 K_1 = 4.797/ln m
ln 2m = ln 2 + ln m
ln m = 2.927
 K_1 = 1.639

Table 3. Linearity experiments, wafer 1

Point	Radius 1	Radius 2	Radius 3	Radius 4	Comments
1	4.365	4.731	4.346	4.553	
2	5.498	5.792	5.559	5.831	
3	6.192	6.563	6.227	6.568	
4	6.863	6.976	6.798	7.246	
5	7.669	7.215	7.184	7.891	Radius 1
6	7.621	7.521	7.544	7.837	Questionable
7	7.755	7.997	7.750		
8	7.996	8.059	8.000		
9	8.183	8.295	8.448		
10	8.321	8.470	8.597		
11	8.522	8.652	8.660		
12	8.662	8.742	8.909		
13	8.820	8.897	9.019		
14	8.959	9.028	9.156		
15	9.142	9.103	9.312		
16	9.265	9.222	9.464		
17	9.434	9.575	9.493		
Ring	9.698	9.716	9.613		
Correction	0.294	0.276	0.379		$E_{i} = 9.992$

Table 4. Ring corrected results, wafer 1

Point	Radius 1	Radius 2	Radius 3	Average	Variance (percent)
1	4.659	5.007	4.725	4.797	4.4
2	5.792	6.068	5.938	5.933	2.4
3	6.486	6.839	6.606	6.644	2.9
4	7.157	7.252	7.177	7.193	0.8
5	7.963*	7.491	7.563	7.527	0.5
6	7.915	7.797	7.923	7.878	1.0
7	8.049	8.273	8.129	8.150	1.5
8	8.290	8.335	8.379	8.335	0.5
9	8.477	8.571	8.827	8.625	2.3
10	8.615	8.746	8.976	8.779	2.2
11	8.816	8.928	9.039	8.938	1.2
12	8.956	9.108	9.288	9.087	2.2
13	9.114	9.173	9.398	9.228	1.8
14	9.253	9.304	9.535	9.364	1.8
15	9.436	9.379	9.691	9.502	2.0
16	9.559	9.498	9.843	9.633	2.2
17	9.728	9.851	9.872	9.817	0.9
Ring	9.992	9.992	9.992	9.992	

^{*}Take out in average.

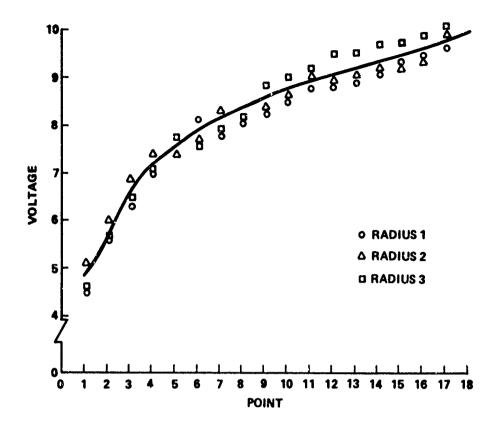


Figure 15. Graph of linearity experiment results.

Data calculated on this basis are shown in column 3 of Table 5.

Using the same type of calculation, column 4 indicates the first and last data fit. Column 3 was calculated on data points 3 and 6 and reveals a much closer fit with measured data.

Column 3 clearly indicates the center contact distortion while column 4 illustrates the conductive ring problem. The last point distortion was surmised to be an error in distance between it and the outer ring. Examination under a microscope proved this to be true.

This phase of experimentation indicated that the material could be held to sufficient isotropic characteristics for the application.

Table 5. Theoretical curve fit, wafer 1

Point	Measurement	Calculation 1 and 2	Calculation 1 and 17	Calculation 3 and 6
1	4.797	4.797	4.797	488
2	4.933	4.933	6.025	5.922
3	6.644	6.598	6.743	6.644
4	7.193	7.0695	7.253	7.156
5	7.527	7.4352	7.648	7.553
6	7.878	7.734	7.792	7.878
7	8.150	7.9866	8.245	8.152
8	8,335	8.2055	8.481	8.390
9	8.625	8.3986	8.690	8.600
10	8.779	8.5713	8.877	8.787
11	8.928	8.7275	9.046	8.937
12	9.087	8.8701	9.200	9.111
13	9.228	9.0012	9.342	9.254
1.4	9.364	9.1228	9.493	9.384
15	9.502	9.2358	9.595	9.509
16	9.633	9.3416	9.709	9.624
17	9.817	9.4410	9.817	9.732
Ring	9.992			

These findings are valid despite the distortion. A further experiment on wafers of this form was planned to verify these results and to further separate problems.

At the same time wafers with one-fourth the number of measurement points along each axis were requested in an attempt to remove the linear distortion. An increase in conductor ring width was made to alleviate the problem caused by ring conductor drop.

III. CONTACT AND FUNCTION EXPERIMENTS

Contact and function experiments were initiated with a number of inherent problems. These problems and the action taken to alleviate them are presented in the following paragraphs.

Considerable distortion was experienced beyond even the second point which apparently resulted from the heating effect. This was countered to some extent by lowering the voltage from 10 to approximately 6 volts therefore reducing power by almost two-thirds.

Ring drop (resulting from current in the conductor) was causing a distortion which could not reasonably be accounted for. Two additional probes were assembled and located around the conducting ring. Observation of resulting data indicated that this maintained the conducting rirg, within measurement tolerance, at equipotential around the circumierence.

The center-located (current insertion) probe destroyed the aluminum deposit because of a constant necessity for manipulation. The probe used was filed to round the point. The same problem was encountered in sample one of this phase but further work on the probe

alleviated this problem on sample two. It did, however, develop as a source of erratic contact which shall be discussed in the data analysis of this phase.

The problem of wafer contact size and field distortion could not be dealt with because of equipment resources. A method of countering this problem will be discussed in the conclusions and recommendations of this report.

Data taken on waier 1 are tabulated in Table 6. The maximum percent error around the average is 5.5 percent which is within tolerance for this effort.

Table 7 has three columns with the first representing average data from Table 6. The second column represents computed values using points one and two as coincident with an idealized curve. The third column indicates percentage difference. The distortion problem around the center appeared under control with the lower voltage.

Tables 8 and 9 show the corresponding values for wafer 2 and agree reasonably with the wafer 1 test. To evaluate the probe manipulation, problem data were recorded. Figure 16 is a plot of these data and indicates an error bias resulting from this effect.

In an attempt to determine the status of producing a Laplace function with accuracy and prior to part IV, the program shown in Table 10 was constructed. The reasoning for this program is based upon the following equations.

If we wish to represent two decades on the wafer (i.e., 1-10, 10-100) then with 17 contacts:

 $K_D = \frac{17}{100} = 0.17$ contact separation per frequency unit.

Table 6. Contact and function results, wafer 1

Point	Radius 1	Radius 2	Radius 3	Radius 4	Average	Maximum Error Around Average (percent)
Center	6.002	6.002	6.002	6.004		
1	2.383	2.436	2.427	2.420	2.416	-1.4
2	1.810	1.882	1.867	1.847	1.852	-2.27
3	1.536	1.533	1.549	1.540	1.540	+0.58
4	1.285	1.333	1.301	1.311	1.308	+1.91
5	1.125	1.118	1.148	1.136	1.132	+1.41
6	0.975	0.935	0.958	0.954	0.956	+2.5
7	0.870	0.896		0.904	0.890	-2.2
8	0.736	0.739		0.747	0.740	+0.95
9	0.647	0.652		0.662	0.654	+1.22
10	0.576	0.559		0.556	0.564	±2.13
11	0.505	0.487		0.506	0.499	-2.4
12	0.427	0.398		0.409	0.411	+3.9
13	0.376	0.342		0.359	0.359	+4.7
14	0.311	0.289		0.319	0.306	-5.5
15	0.250	0.237		0.245	0.244	-2.9
16	0.207	0.206		0.215	0.219	+2.9
17	0.175	0.165		0.160	0.167	+4.8
Ring	0.047	0.055	0.050	0.050		

Table 7. Theoretical curve fit, wafer 1

Point	Measurement	Points 1 and 2	Error (percent)
1	3.586	3.586	0
2	4.150	4.150	0
3	4.462	4.480	0.4
4	4.694	4.714	0.4
5	4.870	4.896	0.5
6	5.046	5.044	0.04
7	5.112	5.169	1.10
8	5.262	5.278	0.3
9	5.348	5.374	0.5
10	5.438	5.460	0.4
11	5.503	5.537	0.6
12	5.591	5.608	0.3
13	5.643	5.673	0.5
14	5.69ნ	5.734	0.6
15	5.758	5.790	0.6
16	5.793	5.842	0.8
17	5.805	5.891	0.9
Ring	5.952		

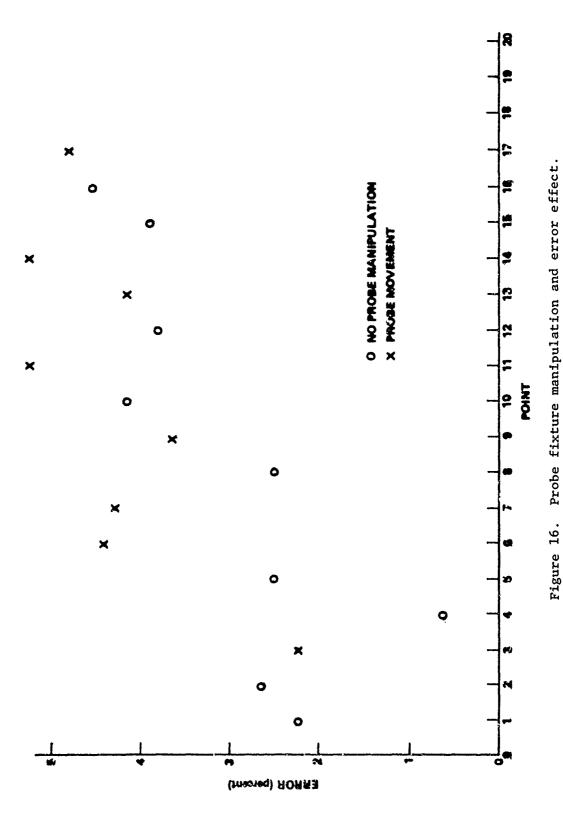
Table 8. Contact and function results, wafer 2

Point	Radius 1	Radius 2	Radius 3	Radius 4	Average	Maximum Error Around Average (percent)
Center	6.342	6.342	6.342	6.342		
1	3 ., 216	3.262	3.248	3.129	3.216	-2.4
2	2.417	2.420	2.416	2.437	2.448	+2.8
3	2.078	2.086*	2.087	2.018*	2.067	-2.4
4	1.726	1.720	1.715	1.654	1.704	-0.73
5	1.417	1.470	1.461	1.469	1.454	-2.5
6	1.306	1.276	1.297	1.318*	1.274	-4.4
7	1.099	1.085	1.146*	1.063*	1.099	+4.3
8	0.935	0.955	0.977	0.967	0.959	-2.5
9	0.793	0.835	0.841	0.784*	0.813	-3.6
10	0.661	0.715	0.702	0.670	0.687	+4.1
11	0.583	0.633*	0.604	0.581*	0.600	+5.5
12	0.476	0.514	0.501*	0.489	0.495	±3.8
13	0.375	0.400	0.395*	0.369*	0.384	-4.1¢
14	0.285	0.294	0.305*	0.275*	0.289	+5.5
15	0.225	0.240	0.242	0.227	0.234	- 3.9
16	0.151	0.163	0.160	0.153	0.153	+4.5
17	0.084	0.085	0.083	0.079*	0.083	-4.8
Ring	0.040	0.041	0.040	0.040		

^{*}Probe adjustment at these measurements.

Table 9. Theoretical curve fit, wafer 2

Pcint	Measurement	Points 1 and 2	Error (percent)
1	3.126	3.126	0
2	3.894	3.894	0
3	4.275	4.342	1.5
4	4.638	4.662	0.5
5	4.888	4.909	0.4
6	5.068	5.111	0.8
7	5.243	5.282	0.7
8	5.383	5.430	0.8
9	5.529	5.560	0.5
10	5.655	5.677	0.4
11	5.742	5.783	0.7
12	5.847	5.879	0.5
13	5.958	5.968	0.2
14	6.053	6.050	0.05
15	6.108	6.126	0.3
16	6.186	6.198	0.2
17	6.259	6.265	0.1
Ring			



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Table 10. Program listing function generation

```
TRANSF
C
   EVALUATION OF BROWN TRANSFER FUNCTION NO. 2
TRAN. FUNC. ==(S-10+J3)(S-4+J6)/(S+3+J7)(S-6+J10)
C
       COMPLEX FU(4),FC(4),S,TFC0,TFC1,TFC13,TFC40
       REAL FMAG(4), FLOG(4), FTRSF, FREG, EXPMF(4), CK2(4), CK3(4), VEXP(17)
      READ 2,FU
    2 FURMAT (8F6.1)
      DO 4 1=1,17
       READ 3, EPOS
    3 FORMAT(5X,F10.3)
    4 VEXP(I) *EPOS
      CK1=1.108
      8*(0.0,-20.0)
       FIND VALUES OF CONSTANTS
C
      00 9 N=1,4
      TFCO=FU(N)
       TFC1=(0.0,1.0)+FU(N)
      TFC13=(0.0,13.0)+FU(N)
       TFG40=(0.0,40.0)+FU(N)
      TFMO=CABS(TFCO)
      TFM1=CABS(TFC1)
       TFM13=CABS(TFC13)
      TFM40=CARS(TFG40)
       TFLN0=ALOG(TFM0)
      TFLN1 = ALOG(TFM1)
      TFLN13*ALGG(TFM13)
      TFLH40=ALOG(TFM40)
      YDEL0=0.17 4TFM0
      TDEL1=0.17+7FM1
      TDEL13=0.17*TFM13
      TDLL40=0.17*TFM40
      IDISO=INT(TOELO)
      IDIS1=INT(TDEL1)
      IDIS13 *INT(TUEL13)
      IDIS40 #INT(TDFL40)
      REMO = TOELO/FLOAT (IDISO )
      REN1=IDEL1/FLOAT(TDIS1;
      REMIS=TDEL13/FLOAT(IDIS13
      REM40 = TDEL40/FLOAT (IDIS40,
      VALO=VEXP(IDISO)+CK1*AL S(REMO)
      VAL1=VEXP(IDIS1)+C' 15 10(RFH1)
VAL13=VEXP(IDIS13') 12 12LOG(REM13)
VAL40=VEXP(IDIS46:-- ,*ALOG(REM40)
      CK2(N)=(TFLN1-TFLNu:/(VAL1-VAL0)
      TEMPA=TFLN40-(VAL40-VEXP(1))*CK2(N)
      TEMPR=Trun13-(VAL13-VEXP(1))*CK2(N)
      CK3(N) * (TEMPA + TEMPB) /2.0
      PRINT 999, CK2(N), CK3(N)
  999 FORMAT (20X, 2F10.4)
    9 CONTINUE
      PRINT 5
    5 FORMAT(1H1,2X113HFREQ
                                    MF1(S) EXPF1(S)
                                                           MF2(8) EXPF2(8)
                             MF4(S) EXPF4(S) CAL.TRS
                                                               EXP, TRS
     XMF3(S)
               EXPF3(S)
    FVALUATE COMPLEX FUNCTION, MODULUS, AND NATURAL LOG.
      DO 20 I=1,49
      00 17 J=1,4
      FC(J)=S+FU(J)
      FMAG(J) = CAHS(FC(J))
```

Table 10. (continued)

AND THE PROPERTY OF THE PROPER

TRANSF FLOG(J) = ALOG(FMAG(J)) DELR=0.17*FMAG(J) IDIST=INT(DELR) IF(IDIST.EQ.O) IDIST=1 REMX=DELR/FLOAT(IDIST) VAL2=VEXP(IDIST)+CK1*ALOG(JEMX) EXPMF(J)=CK2(J)*(VAL2=VEXP(1))+CK3(J) 17 CONTINUE EVALUATE TRANSFER FUNCTION FTRSF=FLOG(1)+FLOG(2)-FLOG(3)-FLOG(4) EXPTR=EXPMF(1)+EXPMF(2)-EXPMF(3)-EXPMF(4) VTRSF=EXP(FTRSF) VXPTR=EXP(EXPTR) ERROR*((VTRSF=VXPTR)/VTRSF)*100.0 FREQ=AIMAG(S) PRINT 99, FREQ, (FLOG(K), EXPMF(K), K=1,4), VTRSF#VXPTP, ERROR 99 FORMAT(2X,F6.1,10F10.4,F9.1) IF(I.GE.41) GO TO 19 S=S+(0.0,1.0) **GO TO 20** 19 8=8+(0.0,10.0) 20 CONTINUE STOP END 0000 ERRORS. COMPILATION COMPLETE. .9025 1.7915 1.7815 .9025 .9025 1.7815 .9025 1.7815

Further using the first two data points on wafer 2,

$$K_1$$
 ln m = 3.126
 K_1 ln 2m = 3.894
 K_1 = 1.108
ln m = 2.8213

which will allow voltage interpolation between points.

Four functions in the form

$$F(S) = \frac{(S+10-j3)(S+4-j6)}{(S-3-j7)(S+6-j10)}$$

were selected and are listed in Table 11 as follows:

The natural logarithm of each function is listed as a function of frequencies. In the program, scale factors are first calculated as

$$\ln |F(s_1)| - \ln |F(s_1)| = K_2(EXP 1 - EXP 2)$$

and a reference reading as

$$K_3 = \frac{\text{EXP 40 - } \ln|F(s_{40})| + \text{EXP 13 - } \ln|F(s_{13})|}{2}$$

and

EXP
$$40 = \ln Kd |F(s_{40})| m$$

This results in a form of a whole number and some number of decimal places such as:

$$= 1n (A.BCDEF) m$$

=
$$\ln Am + \ln \frac{A \cdot BCDEF}{A}$$

where Am represents the reading at a particular point and the second term is an interpolation factor.

Table 11. Computer function generation

-20.0 3.2221 3.2199 3.2698 3.2577 3.3020 3.2899 3.4208 3.41 -19.0 3.1850 3.1828 3.2315 3.2194 3.2647 3.2266 3.3883 3.37 -18.0 3.1467 3.1046 3.918 3.1797 3.2260 3.2139 3.3547 3.3 -17.0 3.1073 3.0552 3.1504 3.0984 3.1858 3.1737 3.3199 3.35 -17.0 3.1073 3.0552 3.1504 3.0984 3.1858 3.1737 3.3199 3.35 -16.0 3.0647 3.0246 3.1073 3.0553 3.1439 3.0084 3.2469 3.22 -15.0 3.0249 2.9828 3.0823 3.0103 3.1003 3.0482 3.2469 3.2 -15.0 3.0249 2.9828 3.0823 3.0103 3.1003 3.0482 3.2469 3.2 -14.0 2.9818 2.9397 3.0153 2.9853 3.0503 3.0026 3.2084 3.16 -12.0 2.9375 2.9954 2.9661 2.9141 3.0069 2.9848 3.1684 3.15 -12.0 2.9375 2.9954 2.9661 2.9141 3.0069 2.9848 3.1684 3.15 -12.0 2.8919 2.0498 2.9145 2.8625 2.9868 2.9047 3.1269 3.00 -11.0 2.7974 2.8169 2.8029 2.8125 2.8485 2.8581 3.0388 2.99 -9.0 2.7486 2.7681 2.7424 2.7520 2.7899 2.7996 2.9920 2.99 -8.0 2.6991 2.7186 2.6783 2.6619 2.6198 2.6615 2.6711 2.8919 2.6687 2.6029 2.8125 2.8885 2.8581 3.0388 2.99 -9.0 2.7486 2.7682 2.6687 2.76783 2.66198 2.6615 2.6711 2.8919 2.86 -5.0 2.59992 2.6188 2.5376 2.5472 2.55909 2.6005 2.8384 2.8 -5.0 2.5499 2.5685 2.4600 2.4696 2.5152 2.5248 2.7833 2.73 -4.0 2.5020 2.8215 2.3768 2.3864 2.4338 2.4434 2.7334 2.73 -4.0 2.5020 2.8215 2.3768 2.3864 2.4338 2.4434 2.7334 2.73 -4.0 2.5020 2.8215 2.3768 2.3864 2.4338 2.4434 2.7334 2.73 -4.0 2.3076 2.3967 2.2971 2.2966 2.3467 2.3553 2.6615 2.5615 2.5248 2.36615 2.36615 2.36615 2.36615 2.3766 2.3967 2.3271 1.8568 1.8664 1.9033 1.9129 2.3166 2.3271 1.8568 1.8664 1.9033 1.9129 2.3161 2.33 -1.0 2.3076 2.3271 1.8568 1.8664 1.9033 1.9129 2.3016 2.3367 2.3271 1.8568 1.8664 1.9033 1.9129 2.3016 2.3066 2.3367 2.3571 1.4566 1.8662 1.9086 1.1002 2.3169 2.3463 2.445 2.3376 2.3271 1.8568 1.8664 1.9033 1.9129 2.3016 2.3367 2.3271 1.8568 1.8664 1.9033 1.9129 2.3016 2.3367 2.3271 1.8568 1.8664 1.9033 1.9129 2.3016 2.3367 2.3271 1.8568 1.8664 1.9033 1.9129 2.3016 2.3367 2.3271 1.8666 1.8662 1.9086 1.1002 2.3367 2.3361 2.3362 2.3361 2.3362 2.3364 2.3362 2.3364 2.3362 2.3364 2.3362 2.3364 2.3362 2.3364 2.3362 2.3364 2.3362 2.3364	====	REQ	MF1(8)	EXPF1(3)	MF2(9)	EXPF2(5)	MF3(8)	EXPF3(S)	MF4(3)	EXPF4(S
										3.37
-17.0 3,1073 3,0652 3,1504 3,0984 3,1858 3,1737 3,3199 3,2840 3,22 -15.0 3,0249 2,9828 3,0623 3,0103 3,0034 3,0482 3,2469 3,22 -14.0 2,9818 2,9377 3,0183 2,9661 2,9141 3,0069 2,9548 3,1684 3,12 -12.0 2,9378 2,9954 2,9661 2,9141 3,0069 2,9548 3,1684 3,12 -12.0 2,8919 2,6498 2,9145 2,8627 2,9964 2,8586 3,0024 3,0833 3,0848 3,0069 2,9548 3,1684 3,12 -11.0 2,7374 2,8169 2,8029 2,8125 2,9568 2,9547 3,1269 3,003 -10.0 2,7374 2,8169 2,8029 2,8125 2,8485 2,8581 3,0388 2,994 -5.0 2,7486 2,7681 2,7424 2,7520 2,7899 2,7952 2,9920 2,994 -6.0 2,5991 2,7186 2,6783 2,6879 2,7277 2,9431 2,859 -7.0 2,6492 2,6687 2,6102 2,6198 2,6615 2,6711 2,8919 2,839 -6.0 2,5992 2,6188 2,5376 2,5472 2,5099 2,6005 2,8384 2,859 -6.0 2,5992 2,5188 2,5376 2,5472 2,5099 2,6005 2,8384 2,772 -1.0 2,5492 2,5595 2,4600 2,6696 2,5152 2,5240 2,7823 2,772 -1.0 2,4563 2,4759 2,2674 2,2969 2,3467 2,3553 2,6615 2,671 -1.0 2,33768 2,3963 2,0872 2,9968 2,1452 2,1548 2,5286 1,023,487 2,3552 2,6615 2,6712 2,3768 2,3963 2,2006 2,2499 2,2595 2,5506 2,6015 2,311 2,3768 2,3963 2,0872 2,312 2,174 2,331 2,1910 2,2006 2,2499 2,2595 2,5506 2,5615 2,6712 2,331 2,3										3.34
-15.0 3,0249 2,9628 3,0623 3,0103 3,1003 3,0482 3,2449 3,22 -14.0 2,9818 2,9397 3,0153 2,9633 3,0646 3,0026 3,2084 3,15 -13.0 2,9375 2,8954 2,9661 2,9141 3,0069 2,9548 3,1684 3,15 -12.0 2,8919 2,8698 2,9145 2,8627 2,9041 2,8521 3,0838 3,03 -10.0 2,7497 2,8169 2,8029 2,8125 2,8485 2,8581 3,0388 2,96 -9.0 2,7486 2,7681 2,7424 2,7520 2,7899 2,7996 2,9920 2,99 -8.0 2,6991 2,7186 2,6783 2,6879 2,7277 2,7372 2,9431 2,85 -7.0 2,6492 2,6687 2,6102 2,6198 2,6615 2,6711 2,8919 2,83 -6.0 2,5992 2,6188 2,5376 2,5472 2,5509 2,6005 2,8384 2,84 -5.0 2,5992 2,6188 2,5376 2,5472 2,5509 2,6005 2,8384 2,84 -5.0 2,5499 2,5695 2,4800 2,4696 2,5152 2,5248 2,7823 2,75 -4.0 2,5020 2,5215 2,3768 2,3864 2,4338 2,4434 2,7334 2,75 -3.0 2,4563 2,4759 2,2874 2,2969 2,3457 2,3553 2,6615 2,67 -1.0 2,3768 2,3963 2,0872 2,0968 2,1452 2,1548 2,62615 2,67 -1.0 2,3768 2,3963 2,0872 2,0968 2,1452 2,1548 2,62615 2,67 -1.0 2,3768 2,3963 2,0872 2,0968 2,1452 2,1548 2,5261 2,53 -1.0 2,3768 2,3963 1,0756 1,9852 2,0302 2,0398 2,4503 2,46 -1.0 2,3222 2,3417 1,8566 1,8664 1,9033 1,9129 2,3811 2,53 -2.0 2,3076 2,3271 1,6566 1,8664 1,9033 1,9129 2,3811 2,53 -2.0 2,3076 2,3271 1,679 1,6094 1,6190 1,6094 1,6190 2,2213 2,23 -1.0 2,3768 2,3871 1,4799 1,5075 1,4452 1,4548 2,1353 2,14 -1.0 2,3768 2,3873 1,4979 1,5075 1,4452 1,4548 2,1353 2,14 -1.0 2,3768 2,3893 1,466 1,4262 1,0285 1,2921 2,0554 2,096 -1.0 2,3768 2,3871 1,4166 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3871 1,4166 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3893 1,4166 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3871 1,4166 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3871 1,4166 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3871 1,4166 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3871 1,4166 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3893 3,4165 1,4262 1,2625 1,2921 2,0554 2,096 -1.0 2,3768 2,3864 2,2899 2,1452 2,5488 2,3026 2,3149 2,2648 2,							3,1858			3.30
-14.0										3.27
-13.0										
-12.0										
-11.0										
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40.0 3.6462 3.6266 3.5332 3.5236 3.5006 3.4910 3.4208 3.41 50.0 3.8723 3.8494 3.7883 3.7626 3.7636 3.7380 3.7000 3.67 60.0 4.0582 4.0493 3.9917 3.9729 3.9719 3.9530 3.9192 3.88 70.0 4.2157 4.1984 4.1608 4.1503 4.1443 4.1330 4.0993 4.08 80.0 4.3522 4.3627 4.3055 4.2860 4.2913 4.2718 4.2522 4.22 90.0 4.4725 4.4946 4.4319 4.4442 4.4195 4.4317 4.3848 4.38	2	20.0	2.9818	2,9397	2,6783	2,6879	2,5909	2.6005	2,4563	2.46
50,0 3.8723 3.8494 3.7883 3.7626 3.7636 3.7380 3.7000 3.67 60,0 4.0582 4.0493 3.9917 3.9729 3.9719 3.9530 3.9192 3.88 70.0 4.2157 4.1984 4.1608 4.1503 4.1443 4.1338 4.0993 4.08 80.0 4.3522 4.3627 4.3055 4.2860 4.2913 4.2718 4.2522 4.28 90.0 4.4728 4.4946 4.4319 4.4442 4.4195 4.4317 4.3848 4.38										2.98
60,0 4,0582 4,0493 3,9917 3,9729 3,9719 3,9530 3,9192 3,88 70.0 4,2157 4,1984 4,1608 4,1503 4,1443 4,1338 4,0993 4,08 80.0 4,3522 4,3627 4,3055 4,2860 4,2913 4,2718 4,2522 4,22 90,0 4,4728 4,4946 4,4319 4,4442 4,4195 4,4317 4,3848 4,38										
70.0 4.2157 4.1984 4.1608 4.1503 4.1443 4.1339 4.0993 4.08 80.0 4.3522 4.3627 4.3055 4.2860 4.2913 4.2718 4.2522 4.22 90.0 4.4726 4.4946 4.4319 4.4442 4.4195 4.4317 4.3848 4.38										
80.0 4.3522 4.3627 4.3055 4.2860 4.2913 4.2718 4.2522 4.22 90.0 4.4726 4.4946 4.4319 4.4442 4.4195 4.4317 4.3848 4.38		76.0								
90.0 4.4726 4.4946 4.4319 4.4442 4.4195 4.4317 4.3848 4.38										
							4,5331	4.5260	4,5020	4.49
								53		
53										
53										

Table 11. Computer function generation

	MF2(9)	EXPF2(8)	MF3(8)	EXPF3(S)	MF4(8)	EXPF4(8)	CAL, TRS	EXP.TR3	ERROR
``	3,2698	3,2577	3,3020	3,2899	3,4208	3.4112	,7938	,7997	-,7
	3,2315	3,2194	3,2647	3,2526	3.3883	3.3787	.7894	7953	-,7
7	3,1918	3,1797	3,2260	3.2139	3.3547	3.3426	7849	,7617	3.0
•	3,1504	3,0984	3,1858	3.1737	3,3199	3.3079	.7803	.7276	6.8
	3,1073	3,0553	3,1439	3.0919	3,2840	3.2720	.7757	.7528	3.0
	3,0623	3,0103	3,1003	3,0482	3,2469	3,2348	.7711	.7483	3.0
	3,0153	2,9633	3.0546	3.0026	3.2084	3,1963	,7665	.7439	3.0
	2,9661	2,9141	3.0069	2.9548	3,1684	3.1563	.7621	.7396	3.0
	2,9145	2.8525	2,9568	2,9047	3,1269	3,0749	.7578	.7654	-1.0
	2.8602	2,8697	2,9041	2,8521	3.0838	3,0317	7539	.8613	-14.2
	2.8029	2,8125	2.8485	2.8581	3.0388	2,9868	.7504	.8061	-7.4
	2.7424	2.7520	2.7899	2,7995	2,9920	2.9400	.7476	.8031	-7.4
	2,6783	2,6879	2,7277	2,7372	2,9431	2,8910	.7458	.8011	-7.4
	2,6102	2,6198	2.6615	2,6711	2.8919	2.8399	7452	.8005	-7.4
	2,5376	2,5472	2,5909	2,6005	2.8384	2.8450	.7464	.7539	-1.0
	2.4600	2.4696	2.5132	2,5248	2.7823	2,7918	7501	.7576	-1.0
	2,3768	2.3864	2,4338	2,4434	2.7234	2,7330	7570	7646	-1.0
	2,2874	2.2969	2,3467	2.3553	2.6615	2.6711	.7684	,7760	-1.0
	2,1910	2,2006	2.2499	2,2595	2,5965	2.6061	.7857	,7935	-1.0
	2,0872	2,0968	2.1452	2,1548	2,5281	2.5377	.8111	.8192	-1.0
	1.9756	1.9852	2.0302	2,0398	2,4563	2,4659	.8477	.8561	-1.0
	1,8568	1.8664	1,9033	1.9129	2,3811	2.3907	.8999	.9089	91.0
	1,7329	1,7425	1,7632	1.7728	2,3026	2.3122	.9750	.9547	-1.0
ξ.	1,6094	1,6190	1.6094	1,6190	2,2213	2,2309	1.0847	1,0955	-1.0
	1,4979	1,5075	1.4452	1,4548	2.1383	2.1479	1,2485	1,2609	-1.0
r	1.4166	1.4262	1,2825	1.2921	2.0554	2.0650	1,4932	1.5081	-1.0
	1,3863	1.3959	1,1513	1,1609	1.9756	1.9852	1.8314	1,8496	-1.0
<u> </u>	1,4166	1.4262	1.0986	1,1082	1.9033	1.9129	2,2066	2,2286	-1.0
ja Ž	1.4979	1.5075	1,1513	1.1609	1.8444	1.8540	2.5000	2,5250	-1.0
	1.6094	1,6190	1,2825	1,2921	1.8055	1.8151	2,6587	2,6852	-1.0
į	1,7329	1.7425	1.4452	1,4548	1.7918	1.5014	2.7126	2,7396	-1.0
	1,8568	1.8664	1.6094	1,6190	1.8055	1,0151	2,6961	2,7230	-1.0
i	1,9756	1,9882	1.7632	1.7728	1.8444	1.8540	2,6307	2,6570	-1.0
	2,0872	2,0968	1,9033	1,9129	1.9033	1.9129	2,6337	2,5590	-1.0
į.	2,1910	2,2006	2,0302	2.0398	1.9756	1.9852	2.4212	2,4453	-1.0
į.	2,2874	2,2969	2,1452	2,1548	2.0554	2.0650	2.3054	2,3285	-1.0
	2.3768	2.3864	2,2499	2,2595	2.1383	2.1479	2,1944	2.2163	-1.0
*	2.4600	2,4696	2,3457	2,3553	2,2213	2.2309	2.0921	2,1130	-1.0
	2,5376	2,5472	2,4338	2,4434	2,3026	2.3122	2.0000	1,8993	5.0
	2,6102	2,6198	2,5152	2,5248	2,3811	2,3907	1.9181	1,8215	5.0
A Park Street	2,6783	2.6879	2,5909	2.6005	2,4563	2.4659	1.8457	1.7528	5.0
,	3.1918	3,1797	3,1439	3.0919	3,0388	2.9868	1.4465	1,5824	-9.4
۶ ک	3,5332	3,5236	3,5006	3.4910	3,4208	3.4112	1,2943	1.2815	1.0
ř	3,7883	3,7626	3,7636	3,7380	3,7000	3,6705	1,2177	1,2257	-,7
ļ	3,9917	3,9729	3,9719	3,9530	3,9192	3,8863	1,1722	1,2006	-2.4
Š	4,1608	4,1503	4,1443	4,1338	4.0993	4,0888	1,1422	1,1344	.7
ř L	4,3055	4,2860	4,2913	4.2718	4.2522	4.2249	1.1210	1.1542	-3.9
	4,4319	4,4442	4,4195	4.4317	4.3848	4,3854	1.1053	1,1294	-2.2
	4,5442	4,5371	4,5331	4.5260	4,5020	4,4949	1.0931	1,1105	-1.6

All experimental points are then computed in the same manner using these constants as

$$EXP = K_2 EXP \text{ (nearest m)} + K_1 \text{ remainder - } EXP 1 + K_3$$

The F(s) and the EXP F(s) are then computed and listed as CAL.TRS and EXP.TRS, respectively, in Table 11. The final column lists the percentage error between the two. Investigation reveals that the excessive error points are a result of the readings at contact three of the data which is well above all others in error content.

IV. FUNCTION GENERATOR EXPERIMENTS

An experiment was made with three sample wafers of the type illustrated in Figure 17. The data for each sample are given in Tables 12 through 14. The same method of fit to an idealized curve as used in part III produced the respective error for wafers 1 and 3.

Wafer 2 indicated two poor data points at 1 and 3. Raw recording indicated interruption during start (point 1) and reading at point 3.

Comparison of data with samples one and three together with corrected data on two would indicate the outcome to be remarkable for reproduction and accuracy.

$$F(s) = \frac{(S + 10 - j3)(S + 4 - j6)}{(S - 3 - j7)(S + 6 - j10)}$$

was again used with the program in Table 15 to produce Tables 16 through 18 for wafers 1 through 3, respectively. The error column reflects the percentage error between the calculated and extrapolated experimental readings. The accuracy is well above that determined as a goal in early stages.

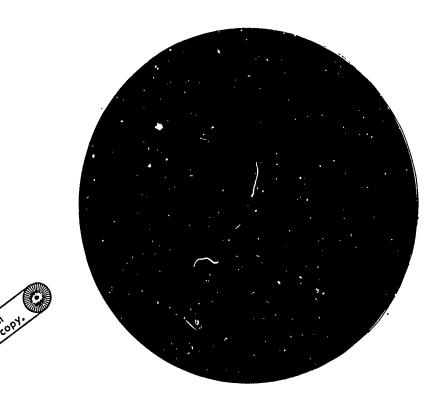


Figure 17. Wafer 1 of the function generator experiments.

Table 12. Function generator results, wafer 1

Point	Reading	K ₁ (ln Pt + ln m)*	Error (percent)
1	3.126	3.126	0
2	4.191	4.191	0
3	4.832	4.814	0.4
4	5.259	5.256	0.06
5	4.476	5.599	0.4
6	5.848	5.879	0.5
7	6.107	6.116	0.1
8	6,298	6.321	0.4
9	6.481	6.502	0.3
10	6.625	6.664	0.6
11	6.782	6.810	0.4
12	6.910	6.944	0.5
13	7.043	7.067	0.3
14	7.150	7.181	0.4
15	7.250	7.286	0.5
16	7.353	7.386	0.4
17	7.454	7.479	0.3

 $*K_1 = 1.5365$ 1n m = 2.03

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Table 13. Function generator results, wafer 2

Point	Reading	Calculation 1 and 2*	Error (percent)	Calculation 2 and 4**	Error (percent)
1	3.126	3.126	0	3.100	0.8
2	4.153	4.153	0	4.153	0
3	4.803	4.754	1.0	4.769	0.7
4	5.206	5.180	0.5	5.264	0
5	5.536	5.510	0.5	5.545	0.2
6	5.806	5.781	0,4	5.822	0.3
7	6.065	6.014	5.0	6.056	0.1
8	6.236	6.207	0.5	6.259	0.4
9	6.422	6.381	0.6	6.438	0.2
10	6.585	6.537	0.7	6.598	0.2
11	6.725	6.679	0.7	6.743	0.3
12	6.867	6.808	0.8	6.875	0.1
13	6.983	6.926	0.8	6.996	0.2
14	7.090	7.036	0.8	7.109	0.3
15	7.193	7.138	0.7	7.214	0.3
16	7.284	7.234	0.7	7.312	0.4
17	7.399	7.323	1.0	7.404	0.07

Table 14. Function generator results, wafer 3

Po	int	Reading	Calculation*	Error (percent)
	1	3.126	3.126	0
	2	4.193	4.193	0
	3	4.819	4.817	0.04
	4	5.255	5.260	0.09
	5	5.576	5.603	0.5
	6	5,861	5.884	0.4
	7	6.110	6.121	0.2
	8	6.298	6.327	0.5
	9	6.483	6.508	0.4
	10	6.657	6.670	0.2
	11	6.798	6.817	0.3
	12	6.928	6.951	0.3
	13	7.053	7,074	0.3
	14	7.169	7.188	0.3
	15	7.268	7.294	0.4
	16	7.369	7.394	0.3
	17	7.464	7.487	0.3

Table 15. Final function generator program

PROGRAH	TRANSF
	PROGRAM TRANSF(INPU), GUTPUT)
	C EVALUATION OF BROWN TRANSFER FUNCTION NO. 2
	C TRAN. FUNC. ==(S-10+J3)(S-4+J6)/(S+3+J7)(S-6+J10)
	COMPLEX FU(4).FC(4).S,TFC0.TFC1.TFC13.TFC40
5	RFAL FMAG(4),FLOG(4),FTRSF,FRFO,EXPMF(4),CK2(4),CK3(4),VEXP(17)
	READ 2,FU
	? FORMAT(8F6.1)
	96 20 L=1,3
	0F40 1,CK1,IO
10	1 FORMAT(6X,F10.4,15X,A2)
	PRINT 6.ID.CK1
	F FORMAT(1H1,4×10HWAFER ID =,42,10×3HK1=,F10,4/)
	90 4 I=1+17
	READ 3, FPOS
15	3 FORMAT(5%,F10.3)
	4 VFXP(I)=FPOS
	S=(0.0,-?0.9)
	C FIND VALUES OF CONSTANTS
	70 9 N=1,4
20	TECO=FU(N)
	TFC1=(0.0,1.0)+FU(N)
	TFC13=(0.0,13.0)+FU(N)
	TFC40=(0.0,40.0)+FU(N) TFM0=CA3S(IFC0) TFM1=CADS(IFC1)
	TF40=CA35 (TFC0)
25	TF41=CABS(TFC1)
	TFH0=CA3S(TFC0) TFM1=CA9S(TFC1) TFM13=CA9S(TFC13) TFM40=CA3S(TFC40) TFLN0=ALOG(TFM1) TFLN1=ALOG(TFM1) TFLN13=ALOG(TFM13) TFLN40=ALOG(TFM40)
	TF440=CA35(TFC40)
	TFLNG=ALOG(TFMO)
	TFLN1=ALOG(TFM1)
30	TFLN13=ALOG (TFM13)
	TFLN40=ALOG(TF440)
	TOFL0=9.17*TFM0
	TOEL1=0.17*TFM1
	TOFL13=0.17*TF#13
35	TNFL40=0.17*TFM40
	IDISO=INT(IDCLO)
	IPIS1=INT(TOFL1)
	IPISI3 = INI(TOFLI3)
	ICTS40 = FAT (TOEL40)
40	PF"0=TDELO/FLOAT(TDISO)
	RFM1=TDEL1/FLOAT(IDIS1)
	PFM13=TDFL13/FLOAT(IDIS13)
	96440=10FL49/FL0AT(IPI949)
•	VALO=VCXP(IDISO)+CK1*ALOS(PFHO)
45	VALI=VEX?(IDTS1)+CK1+ALOG:PFH1)
	VAL13=VEXP(TDTS13)+CK1*4L0G(RF"(3)
	VAL40=VEYP(INIS40)+CK1+ALOG(RFM40)
	CK2(N) = (TFLN1-TFLN0) / (VAL1-VALN)
	TEMPA=TELN49-(VAL40-VFXP(1)) *CK?(N)
50	TE4P8=TELN13-(VAL13-VEXP(1)) *CK2(N)
	CK7(N) = (TF40A+TFHP3) /2.0
	PPINT 999,CK2(N),CK3(N)
	999 FOCHAT (20x, 2F19,4)
	9 CONTINUE
55	PRINT 5

Table 15. (continued)

PROGRAH	TRANSF
······································	5 FORMAT(1H0,2X113HF050 HF1(S) FXPF1(S) HF2(S) EXPF2(S)
-	XHF3(S) EXPF3(S) MF4(S) EXPF4(S) CAL.TRS EXP.TRS ERPOY/
	C FVALUATE COMPLEX FUNCTION, MODULUS, AND NATURAL LOG.
	00 20 I=1,49
60	99 17 J=1,4
	FC(J)=S+FU(J)
	FMAG(J)=CABS(FC(J))
	FL3G(J)=4L0G(F'^* 'J))
	OFLR=0.17*FMAG;
65	Inist=int(DELP)
	IF(IDIST.FQ.0) IDIST=: RFMx=DELR/FLOAT(IDIST) VAL 2=VEXP(IDIST) + CK1 * ALOG (RFMX) FXPMF(J) = CK2(J) * (VAL?-VEXP(1)) + CK3(J) 17 CONTINUE C
	REMX=DELR/FLOAT (IDIST)
	VAL 2=VEXP(IDIST) +CK1*ALOG(9FHX)
	FXPHF(J)=CK2(J)+(VAL?-VEX2(1))+CK3(J)
70	17 CONTINUE
	C EVALUATE TO ANSFER FUNCTION
	FT95F=FL06(1)+6(2)-FL06(3)-FL06(4) (xep) 2
	FX7TR=FXPHF(1)+EXPHF(2)-FXPHF(3)-FXPHF(4)
	VTRSF=EXP(FTPSF)
75	VXPTR≃EXP(EXPTP)
	FRPOR=((VTRSF-VXPTO)/VTPSF)*100.0
	FREQUATING(S)
	PPINT 99.FRFO, (FLOC(Y), FXPMF(K), K=1,4), VTRSF, VXPTR, FPROR
••	99 FORMAT(2X,F6.1,10F10.4,F9.1)
80	IF(I.GE.41) GO TO 19
	S=S+(0.0,1.0)
	GO TO 20 19 S=S+(0.0.10.(;
	SO CONTINUE
85	END SOUTHOR

Table 16. Computer function generation, wafer 1

		•						
		K 1 =	1.5365					
FREQ	MF1(S)	FXPF1(S)	MF?(S)	FXPF2(S)	MF3(5)	EXPES(S)	MF4(S)	FXPF4(S)
-20.0	3.2221	3.2341	3.2698	3.2792	3.3020	3.3113	3.4208	3.4134
-19.0	3.1853	3.1970	3.2315	3.2409	3.2647	3.2741	3.3883	3.3808
-18.0	3.1467	3.1685	3.1918	3.2011	3.2260	3.2354	3.3547	3.3640
-17.0	3.1073	3.1291	3.1504	3.1695	3.1858	3.1952	3.3199	3.3293
-16.0	3.0667	3.0885	3.1073	3.1265	3.1439	3.1631	3.2840	3.2934
-15.0	3.0249	3.0467	3.0623	3.0815	3.1003	3.1194	3.2469	3.2563
-14-0	2.9618	3.9036	3.0153	3.0345	3.0546	3.0738	3.2084	3.2177
-13.0	2.9375	2.9593	2.9661	2.9853	3.0069	3.0260	3.1684	3.1778
-12.0	2.0919	2.9137	2.9145	2.9336	2.9568	2.9759	3.1259	3.1461
-11.0	2.8452	2.8553	2.8602	2.8676	2.9041	2.9232	3.0838	3.1029
-10.0	2.7974	2.8074	2.8029	2.8103	2.8485	2.8560	3.0388	3.0580
-9.0	2.7486	2.7587	2.7424	2.7498	2.7899	2.7973	2.9920	3.0111
-8.0	2.6991	2.7092	2.6783	2.6857	2.7277	2.7351	2.9431	2.9622
-7.0	2.6492	2.6593	2.6102	2.6176	2.6615	2.6689	2.8919	2.9111
-6.0	2.5992	2.6093	2.5376	2.5450	2.5909	2.5983	2.8384	2.8458
-5.0	2.5499	2.5600	2.4630	2.4674	2.5152	2.5227	2.7823	2.7897
-4.0	2.5020	2.5121	2.3768	2.3842	2.4338	2.4412	2.7234	2.7308
-3.0	2,4563	2.4664	2.2874	2.2948	2.3457	2.3531	2.6615	2.6689
-2.0	2.4142	2.4243	2.1910	2.1985	2.2499	2.2574	2.5965	2.6039
-1.0	2.3768	2.3859	2.0872	2.0946	2.1452	2.1527	2.5281	2.5356
0.8	2.3457	2.3558	1.9756	1.9831	2.0302	2.0377	2.4553	2.4638
1.0	2.3222	2.3323	1.8568	1.8642	1.9033	1.9108	2.3811	2.3885
2.0	2.3076	2.3177	1.7329	1.7403	1.7632	1.7706	2.3026	2.3100
3.0	2.3026	2.3127	1.6094	1.6169	1.6094	1.6169	2.2213	2.2288
4.0	2.3076	2.3177	1.4979	1.5053	1.4452	1.4526	2.1383	2.1458
5.0	2.3222	2.3323	1.4165	1.4241	1.2825	1.2899	2.0554	2.2629
6.0	2.3457	2.3558	1.3863	1.3937	1.1513	1.1587	1.9756	1,9831
7.0	2.3768	2.3869	1.4166	1.4241	1.0986	1.1061	1.9033	1.9108
9.0	2.4142	2.4243	1.4979	1.5053	1.1513	1.1587	1.8444	1.8519
9.0	2.4563	2.4664	1.6094	1.6169	1.2825	1.2899	1.8055	1.8129
10.0	2.5020	2.5121	1.7329	1.7483	1.4452	1.4526	1.7918	1.7992
11.0	2.5499	2.5600	1.8568	1.5 2	1.6094	1.6169	1.8055 1.8444	1.8129 1.8519
12.0	2.5992	2.6093	1.9756	1.9831	1.7632	1.7706 1.9108	1.9033	1.9108
13.0	2.6492	2.6593	2.0872	2.0946	1.9033	2.0377	1.9756	1.9831
14.0	2.6991	2.7092	2.1910 2.2874	2.1985 2.2948	2.0302 2.1452	2.1527	2.0554	2.0629
15.0	2.7486 2.7974	2.7587 2.8074	2.3768	2.3842	2.2499	2.2574	2.1383	2.1458
16.0	2.8452	2.8553	2.4600	2.4674	2.3457	2.3531	2.2213	2.2288
17.0	2.8915	2.9137	2.5376	2.5450	2.4338	2.4412	2.3026	2.3100
18.0		2.9593	2.6102	2.6176	2.5152	2.5227	2.3811	2.3885
19.6 20.0	2.9375	3.0036	2.6783	2.6857	2.5909	2.5983	2.4563	2.4638
30.0	2.9816 3.3601	3.3721	3.1918	3-2011	3.1439	3.1631	3.0388	3.0580
40.D	-6462	3.6361	3.5332	3.5258	3.5006	3.4932	3.420	3.4134
50.0	3.8723	3.8674	3.7883	3.7900	3.7636	3.7553	3.7000	3.6873
60.0	4.0582	4.0546	3.9917	3.9855	3.9719	3.9657	3.9192	3.9116
70-0	4.2157	4.2074	4.1608	4.1430	4.1443	4.1264	4.0993	4.0814
80.0	4.3522	4.3466	4.3055	4.2908	4.2913	4.2766	4.2522	4.2411
90.0	4.4725	4.4625	4.4319	4.4193	4.4195	4.4068	4.3848	4.3766
100.0	4.5800	4.5686	4.5442	4.5276	4.5331	4.5165	4.5020	4.4855
200,0	,							

Table 16. Computer function generation, wafer 1

SANSON NEWSCORES	1.5365								
	₹F?(S)	FXPF2(S)	MF3(S)	EXPE3(S)	MF4(S)	FXPF4(S)	CAL.TRS	FXP.TRS	ERROR
	3.2699	3.2792	3.3020	3.3113	3.4208	3.4134	.7938	.8094	-2.0
	3.2315	3.2400	3.2647	3.2741	3.3883	3.3808	.7894	.8049	-2.0
9	3.1918	3.2011	3.2260	3.2354	3.3547	3.3640	.7849	.7947	-1.3
Š.	3.1504	3.1695	3.1858	3.1952	3.3199	3.3293	.7803	.7978	-2.2
	3.1073	3.1265	3.1439	3.1631	3.2840	3.2934	.7757	.7854	-1.3
ja.	3.0623	3.0815	3.1003	3.1194	3.2469	3,2563	.7711	.780 R	-1.3
Ž.	3.0153	3.0345	3.0546	3.0738	3.2084	3.2177	.7665	.7761	-1.3
	2.9661	2.9853	3.0069	3.0260	3.1584	3.1778	.7621	.7716	-1.3
ż	2.9145	2.9336	2.9568	2.9759	3.1269	3.1461	.7578	.7599	3
į	2.8602	2.8676	2.9041	2.9232	3.0838	3.1029	.7579	.7384	2.1
Ş.	2.8029	2.8103	2.8485	2.8560	3.0388	3.0580	.7504	.7437	• 9
ž.	2.7424	2.7498	2.7899	2.7973	2.9920	3,0111	•7476	•740ª	• 9
į.	2.6783	2.6857	2.7277	2.7351	2.9431	2.9622	.7458	•7390	• 9
	2.6102	2.6176	2.6615	2.6699	2.8919	2.9111	• 7452	•7385	• 9
3	2.5376	2.5450	2.5909	2.5983	2.8384	2.8458	.7464	.7484	3
Q.	2.4600	2.4674	2.5152	2.5227	2.7823	2.7897	.7501	•7521	3
í	2.3768	2,3842	2.4338	2.4412	2.7234	2.7308	• 7 570	•7590	3
4	2.2874	2.2948	2.3457	2.3531	2.6615	2.6889	.7684	.7704	3
Ì	2.1910	2.1985	2.2499	2.2574	2.5965	2.6039	.7857	•7878	3
Ľ	2.0872	2.0946	2.1452	2.1527	2.5281	2.5356	.8111	.8133	3
3	1.9756	i.9831	2.0302	2.0377	2.4553	2.4638	.8477	·8499	3
Ž.	1.8568	1.8642	1.9033	1.9108	2.3811	2.3885	•8999	•9023	3
Č	1.7329	1,7403	1.7632	1.7706	2.3026	2.3100	•9750	•9776	3
) Li	1.6094 1.4979	1.6159 1.5053	1.6094	1.6169	2.2213	2.2288	1.0847	1.0875	3
	1.4166	1.4241	1.4452 1.2825	1.4526	2.1383	2.1458	1.2485	1.2518	~ • 3
	1.3863	1.3937	1.1513	1.2899 1.1587	2.0554 1.9756	2.0629	1.4932	1.4971	3
	1.4166	1.4241	1.0986	1.1061	1.9033	1.9831 1.9108	1.0314	1.836?	3
3	1.4979	1.5053	1.1513	1.1587	1.8444	1.8519	2.2066 2.5000	2.2125 2.5066	3
£	1.6094	1.6165	1.2825	1.2899	1.8055	1.8129	2.6587	2.6658	3 3
	1.7329	1.7403	1.4452	1.4526	1,7918	1.7992	2.7126	2.7197	3
r c	1.8568	1.8642	1.6094	1.6169	1.8055	1.8129	2.6961	2.7033	3
	1.3756	1.9831	1.7632	1.7706	1.8444	1.8519	2.6307	2.6377	3 3
ŀ	2.0872	2.0946	1.9033	1.9108	1.9033	1.9108	2.5337	2.5404	3
	2.1910	2.1985	2.0302	2.0377	1.9756	1.9831	2.4212	2.4276	3
5	2.2874	2.2948	2.1452	2.1527	2.0554	2.0629	2.3054	2.3115	3
ì	2.3768	2.3842	2.2499	2.2574	2.1383	2.1458	2.1944	5.5005	3
Ŗ	2.4600	2.4674	2.3457	2.3531	2.2213	2.2288	2.0921	2.0976	3
Ĭ	2.5376	2.5450	2.4338	2.4412	2.3026	2.3100	2.0000	2.0289	-1.5
i.	2.6102	2.6176	2.5152	2.5227	2.3811	2.3885	1.9181	1.9458	-1.4
	2.6783	2.6857	2,5909	2.5983	2,4563	2.4638	1.8457	1.8724	-1.4
,	3.1918	3.2011	3.1439	3.1631	3.0388	3.0580	1.4465	1.4222	1.7
,'	3.5332	3.5258	3.5006	3.4932	3.4208	3.4136	1.2943	1.2909	• 3
	3.7683	3.7900	3.7636	3.7653	3.7000	3.6873	1.2177	1.2273	8
	3.9917	3.9855	₹.9719	3.9657	3.9192	3.9116	1.1722	1.1768	4
	4.1503	4.1430	4.1443	4.1264	4.0993	4.0814	1.1422	1.1531	-1.0
	4.3055	4.2908	4.2913	4.2766	4.2522	4.2411	1.1210	1.127?	5
į	4.4319	4.4193	4.4195	4.4058	4.3848	4.3766	1.1053	1.1033	• 2
5	4.5442	4.5276	4.5371	4.5165	4.5020	4.4855	1.0931	1.0988	5

Table 17. Computer function generation, wafer?

		K1=	1.5192						
FREQ	4F1(S)	FXPF1(S)	MF2(S)	EXPES(2)	MF3(S)	EXPES(S)	MF4(S)	FXPF4(S)	CAL.TRS
-20.0	7.2221	3.2273	3.2699	3.2727	3.3020	3.3049	3.4209	3.4178	.7938
-19.0	3.1850	3.190?	3.2315	3.2345	3.2847	3.2577	3.3883	3.3853	.7894
-18.0	3.1467	3.1744	3.1918	3.1947	3.2260	3.2290	3.3547	3.3576	.7849
-17.0	3.1073	3.1350	3.1504	3.1757	3.1858	3.1887	3.3199	3.3229	.7803
-16.0	3.0667	3.0944	3.1073	3.1327	3.1439	3.1693	3.2840	3.2870	.7757
-15.0	3.0249	3.0525	3.1623	3.0877	3.1003	3.1256	3.2469	3.2498	.7711
-14.0	2.9818	3.0095	3.0153	3.0407	3.0546	3.0800	3.2084	3.2113	.7655
-13.0	2.9375	2.9651	2.9661	2.9915	3.0059	3.0322	3.1584	3.1714	.7621
-12.0	2.8919	2.9196	2.9145	2.9398	2.9568	2.9821	3.1269	7.1523	.7578
-11.0	2.8452	2.8594	2.9602	2.8631	2.9041	2.9294	3.0938	3.1091	.7539
-10.0	2.7974	2.8026	2.8029	2.8059	2.8485	2.8515	3.0388	3.0642	.7504
-9.0	2.7486	2.7539	2.7424	2.7454	2.7899	2,7928	2.9920	3.0173	.7476
-8.0	2.6991	2.7044	2.5783	7.6813	2.7277	2.7306	2.9431	2.9684	.7458
-7 . 0	2.6492	2.6544	2.6102	2.6131	2.6615	2.5645	2.8919	2.9173	.7452
-6.0	2.5992	2.6045	2.53/5	2.5405	2.5909	2.5939	2.8384	2.8413	.7464
-5.0	2.5499	2.5552	2.4600	2.4630	2.5152	2.5182	2.7823	2.7852	.7501
-4.0	2.5020	2.5072	2.3768	2.3798	2,4338	2.4367	2.7234	2.7263	.7570
-3.0	2.4563	2.4616	2.2874	2.2903	2 - 3457	2.3437	2.6615	2.6645	.7684
-2.0	2.4142	2.4194	2.1910	2.1940	2.2499	2.2529	2.5965	2.5994	.7857
-1.0	2.3768	2.3821	2.0872	2.0902	2.1452	2.1482	2.5281	2.5311	.8111
0.0	2.3457	2.3510	1.9756	1.9788	2.0302	2.0332	2.4563	2.4593	.8477
1.0	2.3222	2.3275	1.8568	1.8598	1.9033	1.9063	2.3811	2.3841	.8999
2.0	2.3076	2.3128	1.7329	1.7358	1.7632	1.7662	2.3026	2.3056	.9750
3.0	2.3026	2.3079	1.6094	1.6124	1.6094	1.6124	2.2213	2.2243	1.0847
4.0	2.3076	2.3128	1.4979	1.5008	1.4452	1.448?	2.1383	2.1413	1.2455
5.0	2.3222	2.3275	1.4166	1.4196	1.2825	1.2855	2.0554	2.0584	1.4932
6.0	2.3457	2.3510	1.3863	1.3893	1.1513	1.1543	1.9756	1.9786	1.8314
7.0	2.3768	2.3821	1.4166	1.4196	1.0986	1.1816	1.9033	1.9063	2.2066
8.0	2.4142	2.4194	1.4979	1.5008	1.1513	1.1543	1.8444	1.8474	2.5000
9•0	2.4563	2.4616	1.5034	1.6124	1.2825	1.2855	1.8055	1.8084	2.6587
10.0	2.5020	2.5072	1.7329	1.7358	1.4452	1.4482	1.7918	1.7947	2.7126
11.0	2.5499	2.555 <i>2</i>	1.9568	1.8598	1.5094	1.6124	1.8055	1.8084	2.6961
12.0	2.5992	2.6045	1.9756	1.9786	1.7632	1.7662	1.8444	1.84 3	2.6307
13.0	2.6492	2.6544	2.0872	2.0902	1.9033	1.9063	1.9033	1.91	2.5337
14.0	2.6991	2.7044	2.1910	2.1940	2.0302	2.0332	1.9756	1.9780	2.4212
15.0	2.7486	2.7530	2.2874	2.2903	2.1452	2.1482	2.0554	2.0584	2.3054
16.0	2.7974	2.8026	2.3768	2.3798	2.2499	2.2529	2.1383	2.1413	2.1944
17.0	2.8452	2.8504	2.4600	2.4630	2.3457	2.3487	2.2213	2.2243	2.0921
18.0	2.8919	2.9196	2.5376	2.5405	2.4378	2.4367	2.3026	2.3156	2.0000
19.0	2.9375	2.9651	2.6102	2.6131	2.5152	2.5182	2.3811	2.3841	1.9181
20.0	2.9818	3.0095	2.5783	2.6813	2.5919	2.5939	2.4563	2.4593	1.8457
30.0	3.3601	3.3654	3.1918	3.1947	3.1439	3.1697	3.0388	3.0642	1.4465
40.0	3.6462	3.6409	3.5332	3.5303	3.5006	3.4976	3.4208	3.4178	1.2943
50.0	3.8723	3.8624	3.7883	4.1525	3.7635	4.1278	3.7000	3.6924	1.2177
60.0	4.0582	4.0530	3.9917	3.9842	3.9719	3.9643	3.9192	3.9070	1.1722
70.0	4.2157	4 • 20 5 2	4.1508	4.1552	4.1443	4.1386	4.0993	4.0937	1.1422
80.0	4.3522	4.3485	4.3055	4.3032	4.2913	4.2890	4.2522	4.2434	1.1210
90.0	4.4725	4.4651	4.4319	4.4223	4.4195	4.4898	4.3848	4.3788	1.1053
100.0	4.5800	4.5668	4.5442	4.5333	4.5331	4.5222	4.5020	4.4911	1.9931

Table 17. Computer function generation, wafer?

							·		
K1=	1.5192								
K1= (1(S)	4F2(S)	FXPF2(S)	HE7/C1	EV0E2(6)	WEL (S)	EXDE(* 16)	CAL TOC	CVD IDS	EDD00
1131	756 (3)	- XPF2(\)	HF3(S)	EXPF3(S)	MF4(S)	FXPF4(S)	CAL.TRS	FXP.TRS	ERROR
2273	3.2699	3.2727	3.3020	3.3049	3.4208	3.4178	.7938	.8004	8
1902	3.2315	3.2345	3.2647	3.2677	3.3893	3.3853	.7894	.7759	8
190? 1744	3.1919	3.1947	3.2260	3.2290	3.3547	3.3576	.7849	.8045	-2.5
1350	3.1504	3.1757	3.1858	3.1887	3.3199	3.3229	.7893	.8180	-4.8
0944	3.1073	3.1327	3.1439	3.1693	3.2840	3.2871	.7757	.7951	-2.5
0525	3.9623	3.0877	3.1003	3.1256	3.2469	3.2498	.7711	.7904	-2.5
0095	3.0153	3.0407	3.0546	3.0800	3.2084	7.2113	.7665	.7857	-2.5
9691	2.9661	2.9915	3,0059	3.0322	3.1684	3.1714	.7621	.7812	-2.5
9196	2.9145	2.9398	2.9568	2.9821	3.1269	7.1523	.7578	.7596	2
8504	2.9602	2.8631	2.9041	2.9294	3.0838	3.1091	.7539	.7225	4.2
8026	2.8029	2.8059	2.8485	2.8515	3.0388	3.064	.7504	.7355	2.0
7539	2.7424	2,7454	2.7899	2.7928	2.9920	3.0173	.7476	.7328	2.0
7044	2.5783	2.5813	2.7277	2.7306	2.9431	2.9684	.7458	.7309	2.0
6544	2.6102	2.5131	2.6615	2.5645	2.8919	2.9173	.7452	.7304	2.0
6045	2.5376	2.5405	2.5989	2.5939	2.8384	2.8413	.7464	.7482	2
5552	2.4600	2.4630	2.5152	2.5182	2.7823	2.7852	.7501	.7518	2
5072	2.3768	2.3798	2.4338	2.4707	2.7234	2.7263	.7570	.7588	2
4615	2.2874	2.2903	2.3457	2.345/	2.6615	2.6645	.7684	.7702	2
4615 4194	2.1910	2.1940	2.2499	2.2529	2.5965	2.5994	.7857	.7875	2
3821	2.0872	2.0902	2.1452	2.1482	2.5281	2.5311	8111	.8130	2
*******	1.9756	1.9786	2.0302	2.0332	2.4563	2.4593	.8477	.8496	2
3275	1.8568	1.8598	1.9033	1.9063	2.3811	2.3841	8999	.9020	2
3128	1.7329	1.7358	1.7632	1.7662	2.3025	2.3056	.9750	.9772	?
3079	1.6094	1.6124	1.6094	1.6124	2.2213	2.2243	1.0847	1.0872	2
3128	1.4979	1.5008	1.4452	1.4482	2.1383	2.1413	1.2485	1.2513	2
3275	1.4166	1.4196	1.2825	1.2855	2.0554	2.0584	1.4932	1.4966	-•2
3510	1.3863	1.3893	1.1513	1.1543	1.9756	1.9786	1.8314	1.8356	2
3821	1.4166	1.4196	1.0996	1.1016	1.9033	1.9063	2.2066	2.2117	2
4194	1.4979	1.5008	1.1513	1.1543	1.8444	1.8474	2.5000	2.5058	2
4616	1.6034	1.5124	1.2825	1.2855	1.8055	1.8084	2.6587	2.6648	2
5072	1.7329	1.7358	1.4452	1.4482	1.7918	1.7947	2.7126	2.7188	
5552	1.9568	1.8598	1.6094	1.6124	1.8055	1.8084	2.6961	2.7023	2
6045	1.9756	1.9786	1.7632	1.7662	1.8444	1.8474	2.6307	2.6367	2
6544	2.0872	2.0902	1.9033	1.9063	1.9033	1.9053	2.5337	2.5395	- • 2
7044	2.1910	2.1940	2.0302	2.0332	1.9756	1.9786	2.4212		2
7530	2.2874	2.2903	2.1452	2.1482	2.0554	2.0584		2.4267	-•2
8026	2.3768	2.3798	2.2499	2.2529	2.1383		2.3054	2.3107	2
8504	2.4600	2.4630	2.3457	2.3487	2.2213	2.1413	2.1944	2.1994	-•2
9196	2.5376	2.5405	2.4338	2.4367	2.3026	2.2243	2,0921	2.0969	2
9651	2.6102	2.5131	2.5152			2.3056	2.0000	2.0499	-2.5
0095				2.5182	2.3811	2.3841	1.9181	1.9660	-2.5
3654	2.5783 3.1918	2.6813 3.1947	2.5919 3.1439	2.5939	2.4563	2.4593	1.8457	1.8918	-2.5
SA NO	3.5332	3.5303	3.5006	3.1697	3.0388	3.0642	1.4465	1.3862	4.2
6409 8624	3.7883	4.1525	3.7636	3.4976 6.4279	3.4298	3.4178	1.2943	1.2913	• 5
10024 10530	3.7003	3.9842	3.9719	4.1278	3.7000	3.6924	1.2177	1.2149	. 2
2092	4.1608	4.1552	4.1443	3.9643	3.9192	3.9070	1.1722	1.1804	• • 7
3485	4.3055	4.3032	4.2913	4.1386	4.0993	4.0937	1.1422	1.1412	- 1
3485 4651	4.4319	4.4223		4.2890	4.2522	4.2434	1.1210	1.1267	5
5669	4.5442	4.5333	4.4195 4.5331	4.4098 4.5222	4.3848 4.5020	4.3788 4.4911	1.1053 1.0931	1.1038 1.0906	.1
	707446	ヤチブコカウ	4.7331	4.7///	4.311/1	u.4V11			9

Table 18. Computer function generation, wafer 3

		K1=	1.5393							·····
FREQ	4F1(S)	FXPF1(S)	MF?(S)	FXPF2(S)	MF3(S)	FXPF3(S)	MF4(S)	FXPF4(S)	CAL.TRS	FχP
-20.0	3.2221	3.2263	3.2698	3.2755	3.3020	3.3077	3-4208	3.4119	.7938	
-19.0	3.1850	3.1892	3.2315	3.2372	3.2647	3.2704	3.3883	3.3794	.7894	•
-18.0	3.1467	3.1554	3.1918	3.1975	3.2260	3.2317	3.3547	3.3604	-7849	•
-17.0	3.1073	3.1160	3.1504	3.1605	3.1858	3.1915	3.3199	3.3256	.7803	•
-16.0	3.0567	3.0754	3.1073	3.1174	3.1439	3.1541	3.2840	3.2897	.7757	•
-15.0	3.0249	3.0336	3.1623	3.0725	3.1003	3.1104	3.2469	3.25?6	.7711	•
-14.0	2.9818	2.9905	3.9153	3.0255	3.0546	3.0648	3.2084	3.2141	. 7665	
-13.8	2.9375	2.9462	2.9661	2.9763	3.0069	3.0170	3.1684	3.1741	.7621	•
-12.0	2.8919	2.9006	2.3145	2.9246	2.9568	2,9569	3.1269	3.1371	.7578	•
-11.0	2.8452	2.8527	2.8602	2.8691	2.9041	2.9142	3.0838	3.0939	.7539	•
-10.0	2.7974	2.8049	2.4029	2.9118	2.8485	2.8575	3.0388	3.0490	.7504	•
-9.0	2.7486	2.7561	2.7424	2.7513	2.7899	2,7988	2.9920	3.0021	.7476	•
-8.0	2.6991	2.7066	2.6783	2.6872	2.7277	2.7366	2.9431	2.9532	.7458	
-7.0	2.6492	2.6567	2.6132	2.6191	2.6615	2.6704	2.8919	2.9021	.7452	•
-6.0	2.5992	2.6057	2.5376	2.5465	2.5999	2.5998	2.8384	2.8473	.7464	
-5.0	2.5499	2.5574	2.4600	2.4689	2.5152	2.5241	2.7823	2,7912	.7501	
-4.0	2.5020	2.5095	2,3768	2.3857	2.4338	2.44?7	2.7234	2.7323	.7570	
-3.0	2.4563	2.4638	2.2874	2.2963	2.3457	2.3546	2.6615	2.6704	.7684	
-2.0	2.4142	2.4216	2.1910	2.1999	2.2499	2.2588	2,5965	2.6054	.7857	
-i.0	2.3768	2.3843	2.0872	2.0961	2.1452	2.1541	2.5281	2.5371	.8111	•
0.0	2.3457	2.3532	1.9756	1.9845	2.0302	2.0391	2.4563	2.4652	.8477	•
1.0	2.3222	2.3297	1.3568	1.8657	1.9033	1.9122	2.3811	2.3900	.8999	•
2.0	2.3076	2.3150	1.7329	1.7418	4.7632	1.7721	2.3026	2.3115	.9750	•
3.0	2.3026	2.3101	1.6094	1.6183	1.6094	1.6183	2.2213	2.2302	1.0847	1.
4.0	2.3076	2.3150	1.4979	1.5068	1.4452	1.4541	2.1383	2.1472	1.2485	1.
5.0	2.3222	2.3297	1.4166	1.4255	1.2825	1.2914	2.0554	2.0643	1.4932	1.
6.0	2.3457	2.3537	1.3863	1.3952	1.1513	1.1602	1.9756	1.9345	1.8314	1.
7.0	2.3768	2.3843	1.4166	1.4255	1.0996	1.1075	1.9033	1.9122	2.2066	2.
8.0	2.4142	2.4216	1.4979	1.5068	1.1513	1.1602	1.8444	1.8533	2.5000	2.
9.0	2.4563	2.4638	1.6094	1.6183	1.2825	1.2914	1.8055	1.8144	2.6587	2.
10.0	2.5020	2.5095	1.7329	1.7418	1.4452	1.4541	1.791,	1.8007	2.7126	2.
11.0	2.5499	2.5574	1.9568	1.8657	1.6094	1.6183	1.8055	1.8144	2.6961	5.
12.0	2.5992	2.6067	1.9756	1.9845	1.7632	1.7721	1.6444	1.8533	2.6307	5.
13.0	2.6492	2.6567	2.0872	2.0961	1.9033	1,9122	1.9033	1.9122	2.5337	2.
14.0	2.6991	2.7066	2.1910	2.1999	2.0302	2.0391	1.9756	1.9845	2.4212	5.
15.0	2.7486	2.7561	2.2874	2.2963	2.1452	2.1541	2.0554	2.0643	2.3054	s.
16.0	2.7974	2.8049	2.3768	2.3857	2.2499	2.2588	2.1383	2.1472	2.1944	2.
17.0	2.8452	2.8527	2.4600	2.4689	2.3457	2.3546	2.2213	2.2302	2.0921	2.
18.0	2.8919	2.9006	2.5376	2.5465	2.4338	2.4427	2.3026	2.3115	2.0000	1.
19.0	2.9375	2.9462	2.6102	2.6191	2.5152	2.5241	2.3811	2.3900	1.9181	1.
20.C	2.9818	2.9905	2.6783	2.6872	2.5909	2.5998	2.4563	2.4652	2.8457	1.
30.0	3,3601	3.3644	3.1918	3.1975	3.1479	3.1541	3.0388	3.0490	1.4465	1.
40.0	3.6462	3.6387	3.5332	3.524.5	3.5006	3.4917	3.4208	3.4119	1.2943	1.
50.0	3.8723	3.8610	3.7883	3.7898	3.7636	3.7652	3.7000	3.6939	1.2177	1.
60.0	4.0582	4.8493	3.9917	3.9843	3.9719	5.9644	3.9192	3.9093	1.1722	i.
70.0	4.2157	4.2108	4.1609	4.1610	4.1443	4.1445	4.0993	4.0995	1.1422	i.
80.0	4.3522	4.3459	4.3055	4.2995	4.2913	4.2853	4.2522	4.2487	1.1710	î.
90.0	4.4725	4.4674	4.4319	4.4283	4.4195	4.4159	4.3848	4.3799	1.1053	i.
100.0	4.5800	4.5713	4.5442	4.5359	4.5331	4.5248	4.5020	4.4937	1.0931	1.

Table 18. Computer function generation, wafer 3

7 3.1554 3.1918 3.1975 3.2260 3.2317 3.3547 3.3604 .7849 .78733 8 3.1160 3.1504 3.1605 3.1858 3.1915 3.3199 3.3256 .7803 .78677 8 3.0754 3.1073 3.1174 3.1439 3.1541 3.2840 3.2897 .7757 .77813 9 3.0336 3.0623 3.0725 3.1003 3.1104 3.2469 3.2526 .7711 .77343	· .										
3.2263		K1=	1.5393								
3,1692 3,2315 3,2372 3,2647 3,2704 3,3887 3,3794 7,7894 7,7997 -1,37 3,1160 3,1504 3,1605 3,1858 3,1915 3,3199 3,3256 7,803 7,7867 -7,781 3,0754 3,1073 3,1174 3,1419 3,1504 3,1605 3,1858 3,1915 3,3199 3,3256 7,803 7,7867 -7,781 3,0754 3,1073 3,1073 3,1174 3,2649 3,2657 7,7711 7,734 -3,380 3,0336 3,0623 3,0725 3,1003 3,1104 3,2649 3,2556 7,711 7,734 -3,380 2,9905 3,015 3,0255 3,0546 3,0648 3,2084 3,2141 7,655 7,639 -3,380 2,9006 2,9161 2,9661 2,9658 2,9658 3,1269 3,1271 7,676 7,644 -3,380 2,9006 2,7145 2,2246 2,9568 2,9569 3,1269 3,1371 7,578 7,756 -1,2260 2,2260 2,2365 2,28527 2,4802 2,8651 2,9041 2,9412 3,0838 3,0939 7,739 7,7510 4,44 2,2246 2,7561 2,7843 2,9020 3,0027 7,764 7485 3,22766 2,7761 2,7424 2,7513 2,7849 2,7983 2,9920 3,0027 7,476 7,457 3,322 2,6567 2,6197 2,6191 2,6615 2,6704 2,8919 2,9021 7,452 7,433 3,22,6667 2,6197 2,6191 2,6615 2,6704 2,8919 2,9021 7,452 7,433 3,22,6667 2,6197 2,6465 2,5999 2,5998 2,8473 7,464 7,454 1,25963 2,7874 2,2663 2,3677 2,3538 2,4677 2,3546 2,6615 2,6706 2,6784 2,2963 2,3687 2,3538 2,4677 2,3538 2,4677 2,3546 2,6615 2,6706 2,6706 7,684 7,672 1,2596 2,3517 2,1466 1,265 1,9038 2,0391 2,4563 2,4552 3,4776 3,665 1,9038 2,3097 3,909 3,909 3,908 3,009		FXPF1(S)	MF?(S)	FXPF2(S)	MF3(9)	FXPF3(S)	MF4(S)	FXPF4(S)	CAL.TRS	FXP.TRS	FRROR
3. 1892 3.2315 3.2372 3.2607 3.2704 3.3837 3.3794 .7894 .7999 -1.3 3. 3.1160 3.1504 3.1605 3.1858 3.1915 3.3199 3.3256 .7803 .7867 7 3. 3.0754 3.1073 3.1174 3.1419 3.1541 3.2840 3.2877 .7757 .7781 3 3. 3.0336 3.0623 3.0725 3.1003 3.1104 3.2649 3.2576 .7711 .7734 3 5. 2.9945 2.9661 2.99763 3.0069 3.0170 3.1684 3.2141 .7665 .7644 3 5. 2.9066 2.9146 2.9246 2.9568 2.9669 3.1269 3.1371 .7578 .7561 3 2. 4007 2.4862 2.8651 2.9041 2.9412 3.0838 3.0939 .7539 .7510 .4 2. 2.8027 2.4602 2.8118 2.8445 2.6577 3.0388 3.0490 .7604 .7485 .3 2. 2.8047 2.7612 2.7473 2.6572 2.7776 2.7366 <td>ĺ</td> <td>3.2263</td> <td>3.2698</td> <td>3,2755</td> <td>3.3020</td> <td>3,3077</td> <td>3.4208</td> <td>3.4119</td> <td>.7938</td> <td>.8043</td> <td>-1.3</td>	ĺ	3.2263	3.2698	3,2755	3.3020	3,3077	3.4208	3.4119	.7938	.8043	-1.3
3.1554 3.1918 3.1975 3.2260 3.2317 3.3564 .7849 .7873 3 3.31100 3.1504 3.1605 3.1688 3.1915 3.3199 3.3256 .7803 .7867 .7767 .7761 3 3.0336 3.0755 3.1003 3.1104 3.2840 3.2897 .7757 .7761 3 3.0336 3.08623 3.0055 3.0049 3.0170 3.1684 3.2141 .7665 .7689 3 3.29905 3.015 3.0255 3.0049 3.0170 3.1684 3.1741 .7621 .7644 3 3.29906 2.9462 2.9668 2.9669 3.1259 3.1371 .7578 .7568 .1 2.8527 2.8691 2.9068 3.1269 3.1371 .7644 244 2.7513 2.7899 2.7988 3.0388 3.099 .7539 .7510 .4 4.28040 2.4029 2.818 2.8472 2.7736 2.9431 2.9527 <td>0</td> <td></td>	0										
3 3.1160 3.1504 3.1605 3.1673 3.1174 3.1639 3.1541 3.2840 3.2897 .7757 .7761 .3 3 3.0336 3.0462 3.0725 3.1003 3.1104 3.2840 3.2826 .7711 .7734 3 3 3.0336 3.0462 3.0725 3.1003 3.1104 3.2840 3.2526 .7711 .7734 3 5 2.9462 2.9661 2.9763 3.0069 3.1268 3.1241 .7661 .7664 3 5 2.9066 2.9145 2.9246 2.9668 2.9669 3.1269 3.1371 .7578 .7568 .1 6 2.9046 2.9462 2.9661 2.9964 2.9669 3.1269 3.1371 .7578 .7568 .1 6 2.8046 2.9661 2.9961 2.9641 2.9142 3.0338 3.0090 .7579 .7658 .1 2.7561 2.7424 2.7513 2.7879 2.7366 2.9931 2.9021 .7576 .7457 .7617 2.7465 2	7										
3 3.0336 3.0725 3.003 3.1104 3.2466 3.2526 .7711 .77343 3 2.9905 3.015 3.0255 3.0546 3.0648 3.2084 3.2141 .7665 .76893 5 2.9462 2.9661 2.9763 3.0069 3.0170 3.1664 3.1741 .7621 .76443 5 2.9462 2.9661 2.9768 2.9568 2.9568 3.1269 3.1371 .7678 .7568 .1 2 2.8527 2.9602 2.6591 2.9568 2.9669 3.1269 3.1371 .7678 .7568 .1 2 2.8049 2.3029 2.4118 2.8486 2.8576 3.0388 3.0990 .7639 .7510 .4 4 2.8049 2.3029 2.4118 2.8486 2.8576 3.0388 3.0900 .7604 .7485 .3 5 2.7066 2.6793 2.6872 2.7277 2.7366 2.9931 2.9952 .7458 .7438 .3 5 2.7066 2.6793 2.6872 2.7277 2.7366 2.9931 2.9952 .7458 .7438 .3 5 2.5576 2.7424 2.7513 2.7899 2.7988 2.99431 2.9952 .7458 .7438 .3 5 2.5577 2.4430 2.4689 2.5152 2.5941 2.8919 2.9011 .7452 .7433 .3 5 2.5577 2.4430 2.4689 2.5152 2.5241 2.7823 2.7912 .7501 .7490 .1 6 2.5599 2.7768 2.357 2.4538 2.4927 2.7234 2.7333 .7570 .7559 .1 7 2.54638 2.2874 2.2963 2.3457 2.3584 2.6615 2.6706 .7684 .7672 .1 7 2.5383 2.0872 2.0961 2.1452 2.1541 2.5281 2.5571 .8111 .8099 .1 7 2.3532 1.9756 1.9845 2.0362 2.0391 2.4563 2.45652 .8477 .8465 .1 7 2.3512 1.9758 1.9845 2.0302 2.0391 2.4563 2.45652 .8477 .8465 .1 7 2.3510 1.4979 1.5088 1.4452 1.4541 2.1383 2.1472 1.2485 1.2467 .1 7 2.3532 1.9756 1.9845 2.0302 2.0391 2.4563 2.45652 .8477 .8465 .1 7 2.3510 1.4979 1.5088 1.4452 1.4591 2.1383 2.1472 1.2485 1.2467 .1 7 2.3510 1.4979 1.5088 1.4452 1.4591 2.1383 2.1472 1.2485 1.2467 .1 7 2.3532 1.9756 1.9845 2.0302 2.0391 2.4563 2.4552 2.3614 1.8314 1.8287 .1 7 2.3510 1.4979 1.5088 1.4452 1.4591 1.9756 1.9845 1.8314 1.8287 .1 7 2.3571 1.4166 1.4255 1.0946 1.16183 1.2605 1.9956 2.3115 .9750 .9736 .1 7 2.3572 1.3768 2.3867 2.2968 2.2958 2.29584 2.2966 2.2035 .1 7 2.4668 2.1910 2.1999 2.2988 2.2988 2.2958 2.3115 .9750 .9736 .1 7 2.3572 1.3768 2.3867 2.2968 2.2958 2.2958 2.3006 2.3115 .9750 .9736 .1 7 2.3572 1.9756 1.9845 2.0867 2.2958 2.2958 2.2958 2.3006 2.3015 .9946 .1 7 2.3573 1.3663 1.9957 1.718 1.1607 1.9033 1.9122 2.2066 2.2035 .1 7 2.4660 2.1910 2.1999 2.0302 2.0391 1.9756 1.8844 1.8553 2.5000 2.4964 .1 7 2.7566 2.1910 2.1999	Š										
3 3.0336 3.0725 3.003 3.1104 3.2466 3.2526 .7711 .77343 3 2.9905 3.015 3.0255 3.0546 3.0648 3.2084 3.2141 .7665 .76893 5 2.9462 2.9661 2.9763 3.0069 3.0170 3.1664 3.1741 .7621 .76443 5 2.9462 2.9661 2.9768 2.9568 2.9568 3.1269 3.1371 .7678 .7568 .1 2 2.8527 2.9602 2.6591 2.9568 2.9669 3.1269 3.1371 .7678 .7568 .1 2 2.8049 2.3029 2.4118 2.8486 2.8576 3.0388 3.0990 .7639 .7510 .4 4 2.8049 2.3029 2.4118 2.8486 2.8576 3.0388 3.0900 .7604 .7485 .3 5 2.7066 2.6793 2.6872 2.7277 2.7366 2.9931 2.9952 .7458 .7438 .3 5 2.7066 2.6793 2.6872 2.7277 2.7366 2.9931 2.9952 .7458 .7438 .3 5 2.5576 2.7424 2.7513 2.7899 2.7988 2.99431 2.9952 .7458 .7438 .3 5 2.5577 2.4430 2.4689 2.5152 2.5941 2.8919 2.9011 .7452 .7433 .3 5 2.5577 2.4430 2.4689 2.5152 2.5241 2.7823 2.7912 .7501 .7490 .1 6 2.5599 2.7768 2.357 2.4538 2.4927 2.7234 2.7333 .7570 .7559 .1 7 2.54638 2.2874 2.2963 2.3457 2.3584 2.6615 2.6706 .7684 .7672 .1 7 2.5383 2.0872 2.0961 2.1452 2.1541 2.5281 2.5571 .8111 .8099 .1 7 2.3532 1.9756 1.9845 2.0362 2.0391 2.4563 2.45652 .8477 .8465 .1 7 2.3512 1.9758 1.9845 2.0302 2.0391 2.4563 2.45652 .8477 .8465 .1 7 2.3510 1.4979 1.5088 1.4452 1.4541 2.1383 2.1472 1.2485 1.2467 .1 7 2.3532 1.9756 1.9845 2.0302 2.0391 2.4563 2.45652 .8477 .8465 .1 7 2.3510 1.4979 1.5088 1.4452 1.4591 2.1383 2.1472 1.2485 1.2467 .1 7 2.3510 1.4979 1.5088 1.4452 1.4591 2.1383 2.1472 1.2485 1.2467 .1 7 2.3532 1.9756 1.9845 2.0302 2.0391 2.4563 2.4552 2.3614 1.8314 1.8287 .1 7 2.3510 1.4979 1.5088 1.4452 1.4591 1.9756 1.9845 1.8314 1.8287 .1 7 2.3571 1.4166 1.4255 1.0946 1.16183 1.2605 1.9956 2.3115 .9750 .9736 .1 7 2.3572 1.3768 2.3867 2.2968 2.2958 2.29584 2.2966 2.2035 .1 7 2.4668 2.1910 2.1999 2.2988 2.2988 2.2958 2.3115 .9750 .9736 .1 7 2.3572 1.3768 2.3867 2.2968 2.2958 2.2958 2.3006 2.3115 .9750 .9736 .1 7 2.3572 1.9756 1.9845 2.0867 2.2958 2.2958 2.2958 2.3006 2.3015 .9946 .1 7 2.3573 1.3663 1.9957 1.718 1.1607 1.9033 1.9122 2.2066 2.2035 .1 7 2.4660 2.1910 2.1999 2.0302 2.0391 1.9756 1.8844 1.8553 2.5000 2.4964 .1 7 2.7566 2.1910 2.1999	7.										
2.4905 3.015 3.0255 3.0546 3.0648 3.2084 3.2141 .7665 .76693 2.49462 2.9661 2.9763 3.0069 3.0170 3.1684 3.1741 .7621 .76443 2.49066 2.3145 2.9246 2.9568 2.9568 3.1269 3.1271 .7578 .7568 .1 2.2.8527 2.94602 2.8651 2.9041 2.9142 3.0838 3.0939 .7539 .7510 .4 2.8049 2.4029 2.4188 2.8485 2.8575 3.0388 3.0939 .7539 .7510 .4 2.8049 2.4029 2.4188 2.8485 2.8575 3.0388 3.0939 .7539 .7510 .4 2.8049 2.4029 2.4188 2.8485 2.9520 3.0022 .7476 .7457 .3 2.7066 2.7612 2.7624 2.7513 2.7899 2.7988 2.9920 3.0022 .7476 .7457 .3 2.2.6567 2.6112 2.6191 2.6615 2.6704 2.8919 2.9921 .7452 .7438 .3 2.2.6057 2.5476 2.5465 2.5909 2.5908 2.8384 2.8473 .7464 .7454 .1 2.5097 2.5776 2.5468 2.3857 2.4338 2.4427 2.7234 2.7323 .7570 .7559 .1 2.5097 2.3768 2.3857 2.4338 2.4427 2.7234 2.7323 .7570 .7559 .1 2.4638 2.2874 2.2963 2.3457 2.3546 2.6615 2.6704 .7454 .7454 .1 2.4638 2.2874 2.2963 2.3457 2.2588 2.5965 2.6054 .7657 .7845 .1 2.4638 2.2874 2.2963 2.3457 2.2588 2.5965 2.6054 .7657 .7845 .1 2.24216 2.1910 2.1999 2.2588 2.5965 2.6054 .7654 .7657 .7845 .1 2.23843 2.0872 2.0961 2.1452 2.1541 2.5261 2.5371 .8111 .8099 .1 2.23937 1.3568 1.8657 1.9033 1.9122 2.3811 2.3910 .8999 .8986 .1 2.23297 1.3568 1.8657 1.9033 1.9122 2.3811 2.3910 .8999 .8986 .1 2.23297 1.7568 1.9667 1.9033 1.9122 2.3811 2.3910 .8999 .8986 .1 2.23297 1.7568 1.9657 1.9068 1.4452 1.4541 2.1583 2.2115 .9750 .9736 .1 2.23937 1.4766 1.4255 1.9966 1.4672 1.7721 2.3026 2.3115 .9750 .9736 .1 2.23937 1.4766 1.4255 1.9966 1.4672 1.79721 .8444 1.8533 2.2006 2.2035 .1 2.24216 1.4979 1.5068 1.4452 1.4541 2.1583 2.2114 2.3910 .8999 .8986 .1 2.23937 1.7568 1.8657 1.9069 1.1667 1.9756 1.9845 1.2366 2.2035 .1 2.4638 1.6094 1.6183 1.2825 1.2914 1.8055 1.8144 2.65687 2.65649 .1 2.23843 1.4166 1.4255 1.0946 1.1075 1.9033 1.9122 2.2066 2.2035 .1 2.44618 1.6094 1.6183 1.2825 1.2914 1.8055 1.8144 2.65687 2.6594 .1 2.23843 1.4166 1.4255 1.0946 1.1075 1.9033 1.9122 2.2066 2.2035 .1 2.24216 1.4979 1.5068 1.4952 1.2914 1.8055 1.8144 2.65687 2.6594 .1 2.25677 2.0874 2.2963 2.3457 2.2499 2.2588 2.1383	9										
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CHAPTER V

RESULTS AND CONCLUSIONS

The development of this report from the experimental aspect has followed a familiar pattern. The early phases involved familiarization with the technical problems followed by partial success with first attempts at construction. The last phase diverged from the normal course in that data exceeded expected accuracy by such a large margin. The final data indicate that the device is feasible and that it is probably well beyond any commonly available equipment in existence today.

It can be concluded that further effort should be expended to a final product. A design is suggested which is justified as a conservative approach.

As a result of experimental data and consultation with personnel in the semiconductor fabrication industry, there is little doubt that a device for amplitude function takeoff can be constructed. Because of limited facilities, a final unit could not be constructed within the scope of this report. However the problems encountered are such that a theoretical design can be made and simulation performed to prove its applicability.

The proposed mechanical design is illustrated in Figure 18 with the 10-1 contact schedule presented in Table 19. The design consists of a 180 to 220 ohms/square wafer with a coating of oxide to prevent deterioration of the surface. The contacts, including the conductive

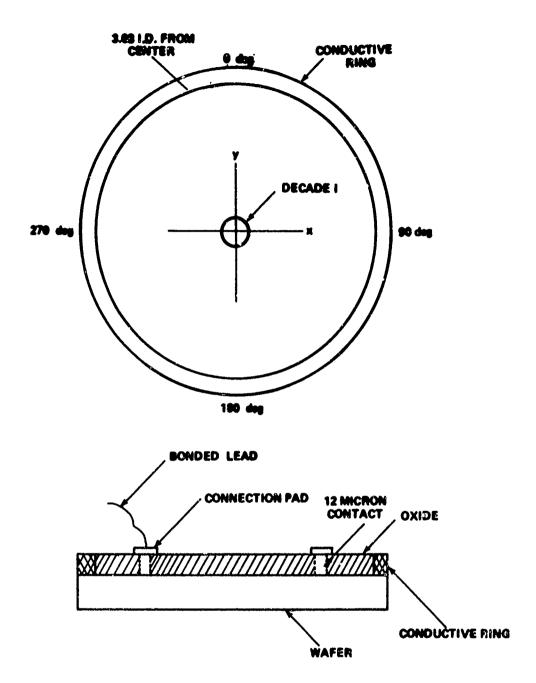


Figure 18. Proposed Laplace function generator wafer design.

Table 19. Wafer design schedule, poles 10 - 1

	Re	1	Re		
W	Xin	Yin	Xin	Yin	
1	0.015	0	0.15	0	
2	-0.015	0.015	-0.15	0.015	
3	0.015	-0.030	0.15	-0.030	
4	0.015	-0.060	0.15	-0.060	
5	-0.015	0.75	-0.15	0.075	
6	0.015	-0.090	0.15	-0.090	
7	-0.015	0.105	-0.15	0.105	
8	0.015	-0.120	0.15	-0.120	
9	-0.015	0.135	-0,15	0.135	
10	0.015	-0.150	0.15	-0.150	
11	-0.015	0.165	-0.15	0.165	
12	0.015	-0.180	0.15	-0.180	
13	-0.015	0.195	-0.15	0.195	
14	0.015	-0.210	0.15	-0.210	
15	-0.015	0.225	-0.15	0.225	
16	0.015	-0.240	0.15	-0.240	
17	-0.015	0.255	-0.15	0.255	
18	0.015	-0.270	0.15	-0.270	
19	-0.015	0.285	-0.15	0.285	
20	0.015	-0.300	0.15	-0.300	(
30	-0.015	0.450	-0.15	0.450	
40	-0.015	-0.600	-0.15	-0.600	
50	-0.015	0.750	-0.15	0.750	
60	-0.015	-0.900	-0.15	-0.900	
70	-0.015	1.05	0.15	1.05	
80	-0.015	-1.20	-0.15	-1.20	
90	-0.015	1.35	-0.15	1.35	
100	-0.015	-1.50	-0.15	-1.50	

ring, are made by penetrating the oxide. This allows use of smaller contacts while the connecting pad can be enlarged above the oxide. A lead is then applied by a bead process to the pad.

It is projected that two real axis poles can be placed on a 3.03-inch wafer, excluding the conductive ring, when arranged in the proper manner.

Then placing two real axis poles, the maximum separation for a near vertical (as apposed to a helix) imaginary axis is obtained by pairing as 10-1, 9-2, 8-3, 7-4, and 6-5.

Data from Chapter IV illustrated that the distortion is within tolerance even with the large pads utilized. Because the distortion is a function of area and displacement, it would appear reasonable that reducing the area factor by 400 would allow for more contacts. It is very likely that a greater number of contacts could be added, thereby reducing the number of wafers required in any given unit. Further experimentation should be conducted to determine the optimum configuration.

In summary experimentation has proven that the amplitude function can be obtained using a thin film semiconductor.

BIBLIOGRAPHY

- 1. Reynolds, C. C. "Amplitude and Phase Response of Generalized Transfer Functions Utilizing a DC-Analog Laplace Transform Generator." Unpublished Master's thesis, The University of Tennessee, Knoxville, 1971.
- Huebschmann, E. C., and C. W. Pender. "Simulation of the Laplace Transform by Means of D. C. Potential in Semiconductor Materials." University of Tennessee Space Institute Report DAAH 1-69-C-1735, Tullahoma, Tennessee, September, 1970.
- 5. Karplus, W. J. Analog Simulation. New York: McGraw-Hill Book Company, Inc., 1958.
- 4. Kayan, C. E. "An Electrical Geometrical Analogue for Complex Heat Flow," <u>Transactions of the ASME</u>, 67:713-718, November, 1945.
- 5. Hicks, H., and A. Permoda. "Uniformly Conductive Surfaces," Engineering Research Institute Report AD-20-135, University of Michigan, Ann Arbor, Michigan, September, 1953.
- 6. Chen, W. H. <u>The Analysis of Linear Systems</u>. New York: McGraw-Hill Book Company, Inc., 1963.

7. Morgan, M. L., and J. C. Looney. "Design of the ESIAC Computer,"

<u>Quarterly IRE Transactions on Electronic Computers</u>,

10 (Part 3):524-529, September, 1961.